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Textured Image Segmentation Using Active Contours

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Abstract. In this paper, we propose a novel level set based active contour model to segment textured images. The proposed method is based on the assumption that local histograms of filtering responses between foreground and background regions are statistically separable. In order to be able to handle texture non-uniformities, which often occur in real world images, we use rotation invariant filtering features and local spectral histograms as image feature to drive the snake segmentation. Automatic histogram bin size selection is carried out so that its underlying distribution can be best represented. Experimental results on both synthetic and real data show promising results and significant improvements compared to direct modeling based on filtering responses.

1 Introduction

Deformable models, particularly active contours, have been widely used for image segmentation and shape extraction due to their natural ability in capturing shape variations [1,2,3,4]. They deform under the influence of internal and external forces to delineate object boundaries. Explicit representations of active contours [5,6] track the points on the curves across time, and hence generally have difficulties in dealing with topological changes, e.g. splitting and merging. Implicit representation based on the level set method [1,2] embeds contours in a higher-dimensional scalar function and deforms the contours through evolving the scalar function, which conveniently facilitates necessary topological changes.

Active contours have been increasingly used in analyzing textured images, e.g. [7,8,9,10]. Despite recent advances in edge based approaches, e.g. [11,12], region based approaches have some obvious advantages when analyzing heavily textured images in that edge based boundary description can easily be compromised by texture patterns. Region based approach generally deforms initial contours towards the region/object boundaries of interest by minimizing an energy function, whose minimum ideally collocates with those boundaries. Thus, it is vitally important to use robust features and region indication/separation functional.

Various features have been investigated in the contour segmentation framework, such as co-occurrence matrices [13], structure tensor [14], and local binary patterns [10]. However, filtering responses are among the most popular approaches, e.g. [15,7,16,17,18]. In [7] the authors decompose the image using Gabor filters. The collected filtering responses at each pixel are used to measure the difference between pixels in a piecewise constant model. However, it largely ignores the spatial distribution

among local filtering coefficients and this direct comparison of filter responses is error prone since the responses can be misaligned due to the anisotropic nature of most of the filters. Wavelet packet transform is used in [16] and the energy distributions in sub-bands are used to characterize textures. One of the main difficulties in dealing with filtering responses is their large dimensionality. It is also challenging to handle textural variations within regions of interest due to, for example, rotation or view point changes, since most of the filters are orientation sensitive.

Once the features are derived, one also needs to decide how to model their distribution so that correct features are included in describing the object of interest. In other words, this modeling provides a region indication or separation functional to drive the active contours. Modeling based on global distribution is a popular approach. For example, in [15,17] Mixture of Gaussians are used to model the image features. Another powerful approach is based on the piecewise constant assumption [19]. It also has been recently adopted in texture segmentation, e.g. [7,18,8]. However, how to cope with texture inhomogeneity is a major challenge.

2   Proposed Approach

In this paper, we propose a novel region based active contour model, which is based on the assumption that local histograms of filtering responses between object of interest and background regions are statistically separable. Briefly, we first apply a bank of filters to the image, from which we have a set of filter responses at different scales and orientations. These responses are then grouped and condensed so that it can handle textural non-uniformity which may occur in real world images. Reduced, invariant features are thus obtained. This process also effectively decreases the dimensionality of filter feature space, which is beneficial for single image segmentation. We then collect local distributions of these features at each pixels, known as local spectral histograms. These local histograms contains not only direct filtering responses but also their spatial distributions in their local neighborhoods. The optimal bin size for these histograms are obtained by minimizing a mean integrated square error based cost function. An energy minimization problem is thus formulated by fitting two spectral histograms, one of which is used to approximate the foreground region and the other for the background. We will show that this approach is effective to handle texture inhomogeneity, compared to, for example, direct modeling based on filtering responses [7] or local intensity distributions [8].

Next, Section 2.1 describes the filter bank and rotation invariant feature selection. Local spectral histogram extraction is presented in Section 2.2 and automatic optimal histogram bin size computation is given in Section 2.3. Finally, Section 2.4 introduces the level set based snake model using these invariant features for image segmentation.

2.1   Filters and Feature Selection

Texture is one of the most important characteristics in identifying objects. It provides important information for recognition and interpolation. Numerous techniques have been reported in the literature to carry out texture analysis. They can be generally categorized in four ways: statistical approaches, which measure the spatial distribution of
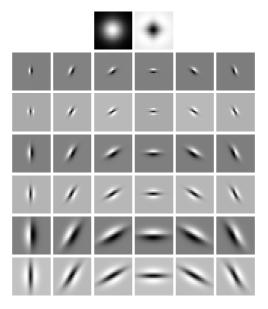
Fig. 1. The filter bank consists 38 filters in total, which include one Gaussian filter, one Laplacian of Gaussian filter, and 36 edge and bar filters across 6 orientations and 3 scales

pixel values, structural approaches, that are based on analyzing texture primitives and the spatial arrangement of these primitives, filter based approaches, which analyze local pixel dependencies using a bank of filters, and model based approaches, which often use derived model parameters as texture features. Filter bank based approaches have been very popular since they can analyze textures in arbitrary orientations and scales and have been strongly motivated by psychological studies of human vision system. They have been shown as an effective approach to classifying [20], segmenting [21] and synthesizing [22] textured images.

However, filter bank based methods often result in high dimensional feature space which can be difficult to handle for certain applications. For example, in [23] the authors found it ineffective to condense the high dimensional Gabor features for the purpose of novelty detection. Unlike image classification, in snake based image segmentation, we may not have enough features extracted from a single image to populate the high dimensional feature space in order to accurately estimate the underlying feature distributions. Moreover, there are usually significant amount of redundant information among the filtering responses. For example, a set of anisotropic filters will get the same responses from isotropic image regions. Fig. 1 shows a bank of filters which has been used in [24] for image classification. It contains two isotropic filters and thirty six anisotropic filters.

The two isotropic filters are Gaussian and Laplacian of Gaussian both with $\sigma = 10$. Those thrifty six anisotropic filters come from two families, edges and bars, each of which consists filters at three progressive scales, i.e. $(\sigma_x, \sigma_y) = \{(1, 3), (2, 6), (4, 12)\}$, and six uniformly spaced different orientations. This moderate size filter bank will produce a thirty eight dimensional feature space, which is considerably large for features extracted from a single image to populate. Fig. 3 gives the filter response images for
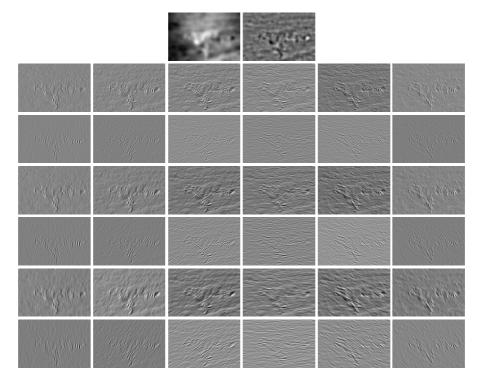
Fig. 2. An example testing image

Fig. 3. Filter responses

the example image shown in Fig. 2. It is evidently clear that there are certain correlations among these filter responses and not all the channels are effectively revealing the image structures. Thus, it is natural to condense the feature space, which is particularly desirable for our application.

It is also worth noting that object in the scene may have inhomogeneous textures due to, for example, perspective projection. This inhomogeneity will exhibit nonuniform responses after applying directional filters, e.g. animal stripe texture (see zebra example
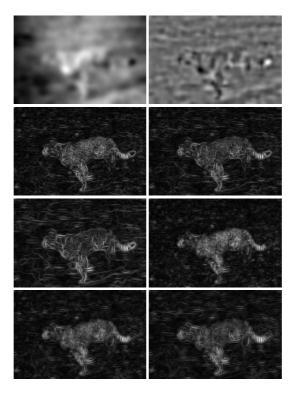
Fig. 4. Maximum filter responses - The first row shows the filter responses from the isotropic Gaussian and Laplacian of Gaussian are kept the same. The rest six filter responses are collected from the 36 directional (isotropic) filter responses. Each of them contains the maximum responses across 6 different orientations (i.e. the six rows of the directional filter responses in Fig. 3 are collapsed into six rotational invariant filter responses).

in Fig. 7) and brick wall texture (see Fig. 8). Rotation invariance is thus desirable in such circumstance. We follow [24] to condense the filter responses by collecting only the maximum filter response across all the six orientations, i.e. those thirty six directional filter responses are reduced to six. Alternative methods, such as steerable filters [25] can also be used. Thus, this not only reduces the dimensionality of the feature space but also simultaneously improve rotational invariancy. Instead of applying convolution operators, the recursive technique [26] is used to efficiently filter the images. Fig. 4 shows the collected maximum responses from those thirty eight filter coefficients. Note the isotropic filter responses are remain unchanged since they are inherently rotationally invariant.

2.2   Local Spectral Histogram

The filtering responses can be directly used to drive the active contours as in, for example, [7]. However, we can further incorporate local spatial dependency of filtering responses by computing the marginal distributions of filter responses over a local window.

Thus, it captures local pixel dependency through filtering and global patterns through histograms. Local spectral histogram has been found useful, for example, texture classification [27]. The maximum filter responses are largely local dominant features, such as edges and bars (e.g. see 4). Their spatial distribution conveys important information regarding the nature of the texture. Misaligning of filter responses due to inhomogeneity of filter responses can be a serious problem for direct approaches. Using local spectral histogram further enhances our model in dealing with texture inhomogeneity and helps to produce more coherent segmentation. Fig. 8 provides an example where directly using filter response without taking into account texture inhomogeneity resulted in a very poor segmentation, whereas the proposed method correctly segmented the foreground object from the texturally nonuniform background.

Let $\mathbf{W}$ denote a local window and $\mathbf{W}^{(\alpha)}(\mathbf{x})$ a maximum filter response patch centered at $\mathbf{x}$, where $\alpha = 1, 2, ..., 8$. Thus, for $\mathbf{W}^{(\alpha)}$ the histogram is defined as [28]:

$$P_{\mathbf{W}}^{(\alpha)}(z_1, z_2) = \sum_{\mathbf{x} \in \mathbf{W}} \int_{z_1}^{z_2} \delta(z - \mathbf{W}^{(\alpha)}(\mathbf{x})) dz, \tag{1}$$

where z_1 and z_2 specify the range of the bin. The spectral histogram is then defined as:

$$P_{\mathbf{W}} = \frac{1}{\mathbf{W}} \left(P_{\mathbf{W}}^{(1)}, P_{\mathbf{W}}^{(2)}, ..., P_{\mathbf{W}}^{(8)}, \right). \tag{2}$$

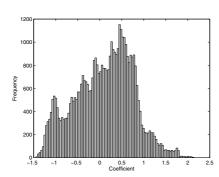Example spectral histograms extracted from the testing image can be found in Fig. 6.

Very recently in [8], local image intensity histogram was used to carry out segmentation in the Chan-Vese piecewise constant framework. However, this method may have difficulties in dealing with highly textured images where intensity alone is not sufficient to describe the texture. Intensity variation, for example, due to illumination variation can also cause severe problems. A comparative example is given in Fig. 9 where the best result reported in [8] is still significantly less accurate than the proposed approach.

2.3   Deducing Optimal Bin Size

Although histogram based methods have been routinely used in various image processing tasks, the importance of automatically selecting appropriate histogram bin size has been largely ignored. However, if a too small bin size is selected, the frequency value at each bin will suffer from significant fluctuation due to the paucity of samples in each bin. On the other hand, if the bin size is chosen too large, the histogram will not be a good representation of the underlying distribution. Thus, it is necessary to select optimal bin size. It also avoids practical problems associated with manual parameter tunning.

We follow the method in [29] to estimate the optimal bin size. Let us consider a histogram as a bar graph. Also, let Δ denote the bin size and Z the range of the coefficients. The expected frequency for $s \in [0, \Delta]$ is:

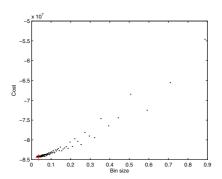$$\theta = \frac{1}{\Delta} \int_0^{\Delta} \lambda_s ds, \tag{3}$$

Fig. 5. Optimal bin size selection - left: A typical spectral histogram for a single maximum response filter; right: The plot shows the relationship between the MISE based cost function and bin size (the red cross indicates the optimal bin size with the lowest MISE value).

where λ_s is the underlying true frequency which is not known. The goodness of fit of the estimated $\hat{\lambda}_s$ to λ_s is measured according to mean integrated squared error (MISE):

$$\text{MISE} = \frac{1}{\Delta} \int_0^{\Delta} \langle E(\hat{\theta} - \lambda_s)^2 \rangle ds, \tag{4}$$

where E denotes expectation and the empirical bar height $\hat{\theta}_i \equiv k_i/\Delta$ (k_i is the frequency count for ith bin). The associated cost function is then defined as:

$$\mathcal{O}(\Delta) = \text{MISE} - \frac{1}{\Delta} \int_0^{\Delta} \langle (\lambda_s - \langle \theta \rangle)^2 \rangle ds. \tag{5}$$

The second term represents a mean squared fluctuation. By assuming the number of events counted in each bin obeys a Poisson distribution, the cost function can be written as:

$$\mathcal{O}(\Delta) = \frac{2}{\Delta} \langle E\hat{\theta} \rangle - \langle E(\hat{\theta} - \langle E\hat{\theta} \rangle)^2 \rangle. \tag{6}$$

The optimal bin size thus is obtained by minimizing the above cost function, i.e.

$$\hat{\Delta} = \arg\min_{\Delta} \mathcal{O}(\Delta). \tag{7}$$

Thus, the testing image is first filtered through the bank of isotropic and anisotropic filters and their responses are condensed into eight channels. Before generating the local spectral histograms at each pixel, global spectral histograms for every eight channels are produced. Then, this optimal bin size selection for each channel is taken place, based on which local spectral histograms are computed. Fig. 5 gives an example of optimal bin size computation.

2.4   Active Contour Based on Wasserstein Distance

The snake based segmentation can be viewed as a foreground-background partition problem (in the case of bi-phase). The snake evolves in the image domain, attempting to

minimizing the feature similarity for those inside and outside the contours. Meanwhile, it tries to minimize the feature difference for those that belong to the same region. Thus, we can formulate our snake based on the piece-wise constant assumption [19,8]. However, since we are using invariant image features and local spectral histograms, the proposed method can cope with texture inhomogeneity much better (see Figs. 8 and 9 as comparative examples).

Let Ω be the image domain, Λ_+ denote the regions inside the snake (foreground) and Λ_- those outside the snake (background). The snake segmentation can be achieved by solving the following energy minimization problem:

$$\inf_{\Lambda_+} \mathcal{E}(\Lambda_+) = \alpha \mathcal{L}(\Lambda_+) + \int_{\Lambda_+} \mathcal{D}(P(\mathbf{x}), P_+) d\mathbf{x} + \int_{\Lambda_-} \mathcal{D}(P(\mathbf{x}), P_-) d\mathbf{x}, \qquad (8)$$

where α is a constant, $\mathcal{L}$ denote length, $\mathcal{D}$ is the metric which measures the difference between two histograms, and P_+ and P_- are the foreground and background spectral histograms to be determined. The first term is the length minimization term which regularize the contour. The next two terms are data fitting terms, which carry out the binary segmentation.

Among many other candidates, such as χ^2 distance and normalized cross correlation, The Wasserstein distance (also known as the earth mover's distance) [30] is used to compute the distance between two normalized spectral histograms. since it is a true metric (unlike χ^2 distance) and has been found very useful in various applications, e.g. image retrieval [30]. Let $H_a(y)$ and $H_b(y)$ be two normalized spectral histograms. The Wasserstein distance between these two histograms is defined as:

$$\mathcal{D}(P_a, P_b) = \int_T |F_a(y) - F_b(y)| dy, \qquad (9)$$

where T denotes the range of the histogram bins, and F_a and F_b are cumulative distributions of P_a and P_b, respectively.

The level set method is implemented to solve this energy minimization problem so that topological changes, such as merging and splitting, can be effectively handled. Let ϕ denote the level set function. The foreground is identified as $\Lambda_+ = \{\mathbf{x} \in \Omega : \phi(\mathbf{x}) > 0\}$, which can be computed using the Heaviside function, i.e. $\int_\Omega \mathcal{H}(\phi) d\mathbf{x}$ where $\mathcal{H}$ is the Heaviside function. The level set formulation can be expressed as:

$$\begin{aligned}
\inf_{\Lambda_+} \mathcal{E}(\Lambda_+) =& \alpha \int_\Omega |\nabla \mathcal{H}(\phi)| d\mathbf{x} \\
&+ \int_\Omega \mathcal{D}(P(\mathbf{x}), P_+) \mathcal{H}(\phi) d\mathbf{x} \\
&+ \int_\Omega \mathcal{D}(P(\mathbf{x}), P_-)(1 - \mathcal{H})(\phi) d\mathbf{x}
\end{aligned} \qquad (10)$$

The regularized Heaviside function proposed in [19] is used to allow larger support in the vicinity of the zero level set so that the contours can be initialized anywhere across the image (e.g. see Fig. 7):

$$\mathcal{H}_\epsilon(z) = \frac{1}{2}\left(1 + \frac{2}{\pi}\arctan(\frac{z}{\epsilon})\right). \qquad (11)$$
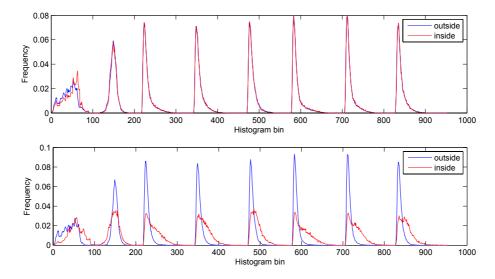
Fig. 6. The average local spectral histogram inside and outside the snake - top: These two histograms are largely overlapping each other; bottom: It clearly shows the difference between the histograms when the snake converged to the object boundaries.

Thus, minimizing $\mathcal{E}$ with respect to ϕ gives us the following partial differential equation:
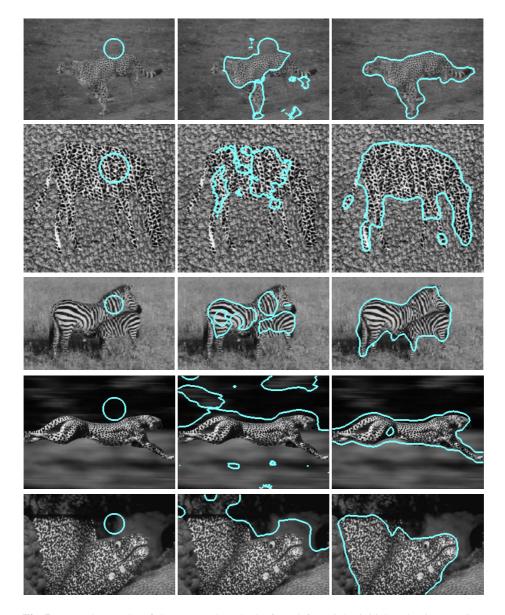
$$
\begin{aligned}
\frac{\partial \phi}{\partial t} =& \delta(\phi)\Big[\alpha\nabla\cdot\left(\frac{\nabla\phi}{|\nabla\phi|}\right) - (\mathcal{D}(P(\mathbf{x}),P_+) - \mathcal{D}(P(\mathbf{x}),P_-))\Big] \\
=& \delta(\phi)\Big[\alpha\nabla\cdot\left(\frac{\nabla\phi}{|\nabla\phi|}\right) \\
& - \int_T |F_\mathbf{x}(y) - F_+(y)|dy + \int_T |F_\mathbf{x}(y) - F_-(y)|dy\Big],
\end{aligned}
\tag{12}
$$

where $\delta(x) = \frac{d}{dx}\mathcal{H}(x)$, F_+ and F_- are the spectral cumulative histogram inside and outside the contours, respectively. The minimization process thus moves the contours towards object boundaries through competing pixels by measuring the similarity of local cumulative spectral histogram with those inside and outside current foreground.

Fig. 6 shows an example of spectral histogram changes between the initial stage and the stabilized result. The corresponding segmentation result can be found in the first row of Fig. 7.

3   Results

The proposed method has been tested on both synthetic and real world images. Fig. 7 shows some typical example results obtained using the proposed method. The first row shows the result of the running example given earlier. Good segmentation was achieved despite the large variations in the body region. In the second example, reasonable result

Fig. 7. Examples results of the proposed method - from left to right: initial snake, intermediate stages, and stabilized result

was obtained, missing some very fine and thin structures. In the third example, there are clearly texture orientation variations. In the last two rows, the initial snakes were placed outside the objects of interest but still managed to localize them. Particularly, in the last example, there are significant texture variations both in foreground and background regions, which made it very difficult to segment.
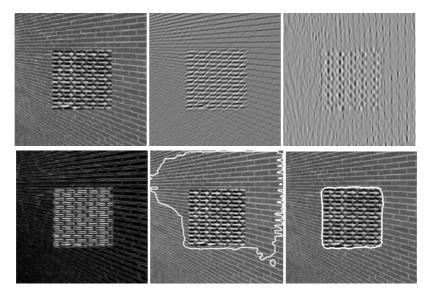
Fig. 8. Top row - a synthetic texture collage which contains an inhomogeneous background due to orientation and scale changes, and two filter responses to particular orientations; Bottom row - the maximum response derived across different orientations which highlights edge features in various directions, including vertical; segmentation result obtained using the Chan-Vese model based on Gabor features [18]; segmentation result obtained using the proposed method.
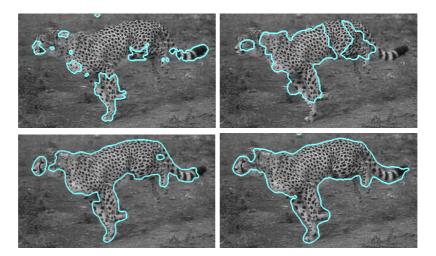

Fig. 9. Comparative analysis. Top row - results obtained using edges based methods, namely geodesic snake and generalized GVF snake [3]; bottom row - the left image shows the best result on the testing image reported in [8] using a region based approach; the last image shows the result obtained using the proposed method.

In Figs. 8 and 9, we mainly compare our work with two extensions of the piece-wise constant model, which is also our fundamental model. Fig. 8 demonstrates when dealing with inhomogeneous textures, the proposed method performs significantly better than that directly using filter responses [7]. The proposed method also showed improvements against a very recent method based on local histograms [8]. It illustrates the effectiveness of using invariant filtering technique. Fig. 9 also gives example results obtained from geodesic snake and generalized GVF snake [3]. It is expected that these edge based techniques are not appropriate when dealing with highly textured images.

The proposed method requires very little parameter tunning. All the images given in this paper are using a fixed set of parameters. The parameters used to generate the filter bank are given in Section 2.1. The local window used to collect the spectral histogram is empirically fixed as 19. For a too small window size, the local spectral histogram may have difficulties in reflecting underlying distribution and can result in isolated regions. For a too large window, the segmentation can be less accurate around object boundaries. We found that a window size of 19 is a good tradeoff, however, we attempt to automatically select the window size as part of our future work. The parameter α controls the smoothness of the contour and very rarely needs to be adjusted.

4 Conclusions

In this paper, we introduced a novel region based snake method which is based on the assumption that foreground and background local filtering response distributions are statistically separable. Maximum response filters were used to achieve rotational invariancy and their local spectral histograms were used as image features to drive the snake. The experimental studies showed some promising results. As part of our future work, we will further investigate optimal filter selection and automatic local spectral histogram window selection.

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