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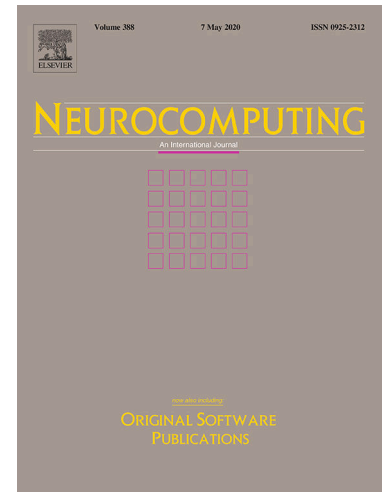
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# Collaboration of Multiple SCARA Robots with Guaranteed Safety Using Recurrent Neural Networks

Yuhong He<sup>a</sup>, Xiaoxiao Li<sup>b</sup>, Zhihao Xu<sup>b</sup>, Xuefeng Zhou<sup>b,\*</sup>, Shuai Li<sup>a,\*</sup>

<sup>a</sup>*School of Engineering, Swansea University, Swansea SA2 8PP, U.K.*

<sup>b</sup>*Guangdong Key Laboratory of Modern Control Technology, Institute of Intelligence Manufacturing, Guangdong Academy of Sciences, Guangzhou, Guangdong 510070, P.R. China*

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## Abstract

SCARA robot is one of the most popularly used robots in industry. The obstacle avoidance feature of multiple SCARA robot collaboration is essential and prominent, which can be used to support multiple robots to accomplish not only more sophisticated tasks but also more efficient than individual robot. This paper mainly focuses on studying the problem of simultaneous multi-robot coordination and obstacle avoidance. A cooperative kinematic control problem of multiple robot manipulators, collision avoidance is taken into account to be the primary task as an inequality constraint and trajectory planning task is considered to be the secondary objective as to ensure the priority of safety, is described as a quadratic programming(QP) problem. Then, a recurrent neural network (RNN) based dynamic controller is designed to solve the formulated QP problem recursively. The convergence of the designed neural network is proved through Lyapunov analysis. With three SCARA planar robots, the effectiveness of the proposed controller is validated through numerical simulations. As observed in the results, when the minimal distance between robots is less than the setting safety distance, the collision avoidance strategy reacts to impel robots to avoid collision, which achieves the primary objective for obstacle avoidance; otherwise, the robot performs the desired trajectory tracking task.

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\*Y. He, X. Li and Z. Xu are jointly first authors. X. Zhou and S. Li are jointly corresponding authors.

\*Corresponding author (xf.zhou@gia.ac.cn; shuai.li@swansea.ac.uk)

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## 1. Introduction

In recent years, robot technology has continuously improved the capabilities of robots, and has constantly expanded the scope of robot applications[1, 2, 3, 4]. While society often **expects** robots can accomplish more sophisticated tasks, these challenges can hardly achieve by **an individual** primitive robot[5]. The superior advantages of multi-robot collaboration are reflected mainly in the wide application field, good fault tolerance, high efficiency and good scalability, which leads for the need of Multi-Robot Coordination. Having said that, path planning, synchronized control, and team formation [6, 7, 8]are crucial fields of diverse robot application features. Thanks to the enhanced reliability of platforms and sensors, as well as the low-cost of technology, robotic platforms are now used widely for sophisticated tasks such as domestic services or industrial **assembly lines**.

Multi-robot systems have been broadly applied to various applications to perform a given task collaboratively and cooperatively[9]. In a multi-robot environment, path-planning or collision avoidance is an important feature[10]. In multi-robot collaborations, **direct collisions** between robots and any collateral damage for technicians will be prevented. Thus, Real-Time obstacle avoiding is the main target. But for non-redundant robots, due to the limitation of **the degree** of freedom, **the robot** cannot physically achieve the motion control task while realizing obstacle avoidance. In view of the above contradiction, we proposed a safety precaution mechanism, **i.e.**, the priority of obstacle avoidance is **superior to** kinematic control.

Obstacle avoidance is a fundamental yet profound design factor of rigorous industrial manipulators. It has been a long journey for scholars studying various methods aiming to solve different scenarios of real applications. According to [11][12], Zhang *et al.* used online quadratic-programming(QP) method to solve

for inverse-kinematic obstacle avoidance control problem. The simulation was based on the PAIO robot(redundant) manipulator in the presence of obstacles. In [13], similarly, Xu *et al.* described the avoidance strategy as QP with general class-K functions to solve QP problem online. The simulation was done on a 4-link planar redundant robot. Both static and dynamic obstacles were there to test for its performance. Khan *et al.* [14] announced an "beetle antennae olfactor" RNN which integrates path tracking control with obstacle avoidance into a optimization problem. The proposed algorithm was proved via simulations done by KUKA LBR 7-DOF industrial manipulator. All of these studies aimed to find solutions via online programming planning, and realized by single robot manipulator as the main object in actual trials. Obstacles are either static or dynamic objects. In factory assembly lines, manipulators often encounter collision risks from other robots or machines. Our study is focusing on multi-robot collaboration scenarios.

On the contrary, the following studies examined multi-robot collaboration control with obstacle avoidance. Both [15] and [16] implemented kinematic controls to solve for optimal trajectory problem with affective algorithms where multi-robot cooperation can be achieved. In [16, 17, 18, 19], authors examined dynamic trajectory planning method of multiple robot manipulators scenario as an optimal control problem. Analogously,[20] researched collaboration of multiple wheeled mobile manipulators by a collision avoidance technique. [21] used another optimization algorithm to solve for trajecotory planning problem of multi-robot formation. [15, 16, 20, 21] negelected to explore an important feature in depth when desgining our multi-robot coordination control system, that is the obstacle avoidance whose function is to ensure safety while in operation with other machines. [22] asserted that by exploiting redundancy and potential function method to avoid collisions when manipulating two cooperative robots. In pursuit of fastness of completion of certain kinematic tasks, we cannot afford to sacrifice safety criterion. Safety shall always be the top priority, and everything else builds upon this foundation. Our research goal is to fulfill secure operation while adding tracking control for multi-robot collaboration on

top of this foundation.

60 Neural networks, combining with artificial intelligence techniques, provide a fresh perspective for robotic formation control.[23]. Planning problem is an important topic for robotics control. It can be categorized as online planning and offline planning[24, 25]: Offline planning lacks of the ability for real-time controlling of manipulators. It is ideally suited for simplex trajectories in static  
65 known environment. In virtue of its rapid response when environments are constantly changing, online planning can handle challenges in unknown dynamic by continually modifying strategies and models[26, 27]. Berkeley Artificial Intelligence Research Lab announced a [full-fledged discovery](#) that a dynamic neural network model-based reinforcement learning algorithm can produce sound and  
70 creditable gaits that accomplish various complex locomotion tasks[28]. [29] is an example of an offline path planning problem. This problem pertains to combinatorial optimization problems. In [30], authors developed a neural network confined by kinematic constraints for mobile robots; The dynamics is identified online by the neural network estimators. Without measuring joint velocities,  
75 a robust online learning neural network output feedback scheme is offered to control motion control of robot manipulators[31].

Neural networks have [various computational methodologies](#) that can be realized to increase processing speed[32, 33]. In studies of [34] and [35], both objectives were to solve for unknown dynamics of manipulators; while the former  
80 used adaptive neural network and the later modified the conventional backpropagation algorithm. In an unknown environment, [36] provides [an effective](#) RNN model for collision-free path planning with limited information of the obstacle positions. Nevertheless, [37] mentions a Lagrangian network(RNN) can be used to deal with obstacle avoidance and trajectory tracking simultaneously knowing  
85 obstacle positions. [38] presents two neural networks of velocity inverse kinematics problem for redundant robots. In each proposed neural network approach, two cooperating recurrent neural networks are used.

Enlightened from the above awareness, we describe the problem of robot kinematic control as an optimization problem, which describes obstacle avoid-

90   ance as an inequality constraint. As stated before, the foundation of multi-robot  
collaboration is based upon safety ensurance. The design intellection is to keep  
the moving error of manipulators running with respect to desired trajectory. Fol-  
lowing this concept, we took a step forward by designing a dynamic(recurrent)  
neural network to solve this problem. Through assigning robot manipulators  
95   as a set of critical points, the distances between the manipulators are approx-  
imately described by a group of point-to-point distances. The obstacle avoid-  
ance problem is then reformulated as a QP problem in the velocity level, and  
a dynamic(recurrent) neural network is designed to solve the QP online. In  
numerical results, we show the experiment results from simulation of 3 Scara  
100   robots to prove the reliability of our method proposed in this paper.

The remainder of this paper is arranged as below. In Section 2, fundamental  
robot kinematics are given, and illustration of obstacle avoidance implication  
are demonstrated with the control objective. In Section 3, original QP formu-  
lation is introduced first, then [an optimization](#) control problem is shown. With  
105   further [in-depth](#) derivations, we summarize a sophisticated constrained opti-  
mization problem. Followed by Section 4 an RNN algorithm is implemented  
for solutions to the inequality constraint and analysis of the tracking error in  
Cartesian space is also discussed. In Section 5, numerical and experimental  
results and comparisons are conducted on three 2-link Scara planar robot ma-  
110   nipulators. Lastly, a comprehensive conclusions are included to summarize our  
overall effort devoted in this work. Before ending the introductory section, we  
highlight the main contributions of this paper as below:

- By the proposed RNN based control scheme, both trajectory tracking and  
collision avoidance can be realized concurrently. Meanwhile, Manipula-  
115   tors' kinematic and dynamic constraints are satisfied. We are able to keep  
manipulators running with pre-defined trajectory while [complying](#) with a  
safe distance between one another.
- An innovative method of obstacle avoidance between multiple SCARA ma-  
nipulators in the form of multi-robot-collaboration system is introduced.

120 The RNN algorithm(QP-based optimization) we designed for this research  
 is capable of simultaneously guaranteeing controlled quantity in real time,  
 and maintaining the stability of the control system.

- The distinction from others is that our method first considers planning  
 collision-free path of multiple planar Scara manipulators, and then takes  
 125 further exploration on physical simulation held by these 2-link robots, par-  
 ticularly to test robot's self-correcting competency when pre-defined path  
 is impacted and minimized the production loss(i.e. machine damages).

## 2. Problem Formulation

In this section, basic knowledges of robot kinematics and obstacle avoidance  
 130 are presented to lay a foundation for latter illustrations.

### 2.1. Robot Kinematics

The forward kinematics of a non-manipulator involves a nonlinear transfor-  
 mation from a joint space to a Cartesian workspace, as described by

$$r(t) = f(\theta(t)). \quad (1)$$

where  $r(t) \in \mathbb{R}^m$  is an  $m$ -dimensional vector in the workspace that describes  
 the position and orientation of the end effector at time  $t$ ,  $\theta(t) \in \mathbb{R}^n$  is an  $n$ -  
 dimensional vector in the joint space, each element of which describes a joint  
 angle, and  $f(\cdot) : \mathbb{R}^n \rightarrow \mathbb{R}^m$  denotes the nonlinear mapping from the joint space  
 to the task space of the manipulator. Because of the nonlinearity of the mapping  
 $f(\cdot)$ , it is usually difficult to directly obtain the corresponding  $\theta(t)$  for a desired  
 $r(t) = r_d(t)$ ,  $r_d(t) : \mathbb{R} \rightarrow \mathbb{R}^m$  is a smooth function defining a desired path to  
 be tracked by the end-effector. By contrast, the mapping from the joint space  
 to the workspace at the velocity level is an affine mapping and thus can be  
 used to significantly simplify the problem, which can be illustrated as follows.  
 Computing the time derivative on both sides of (1) yields

$$\dot{r}(t) = J\dot{\theta}(t). \quad (2)$$

where  $J = \partial(f)/\partial(\theta) \in \mathbb{R}^{m \times n}$  is the Jacobian matrix of  $f(\cdot)$ , and  $\dot{r}(t)$  and  $\dot{\theta}(t)$   
 135 are the Cartesian velocity and the joint velocity, respectively.

## 2.2. Obstacle Avoidance

Generally speaking, obstacle avoidance problem usually contains how to track the desired end-effector trajectory while simultaneously ensuring that **there are** no collisions with any obstacle in the workspace of the manipulator.

140 Similar to game theory phenomenon, each robot can be treated as a individual player, and consider all other robots as obstacles during kinematic operation. Between **the robot**  $i$  and the specific obstacles, there **exists the** closest distance with two fix points. While satisfying kinematic condition, robot  $i$  also has to maintain a safe distance that is further than the closest distance with obstacles.  
 145 Every robot  $i$  cares only about those two objectives, such as the player only acting on his/her behalf.

Let  $Z_1$  be the set of all points on robot  $i$ , and  $Z_2$  be the set of points on obstacle(s), then the goal of obstacle avoidance of a robot manipulator is to constantly satisfy  $Z_1 \cap Z_2 = \emptyset$ . By presenting a safety distance  $d_0$  between the robot and obstacle(s). The obstacle avoidance is formulated as

$$\|p_i^* - p_j^*\| \geq d_0, p_i^* \forall Z_1, p_j^* \forall Z_2 \quad (3)$$

while  $p_i^*, i = 1, \dots, a$  and  $p_j^*, j = 1, \dots, b$  being the vertexes of a specific robot and another vertex of the obstacle(s) within testing environment, respectively. To avoid any possible obstacles the manipulator has to maintain that  $d_{min} \geq d_0$   
 150 as shown in Fig. 1, where  $d_{min} = \|p_i^* - p_j^*\|$  denotes the Euclidean distance of  $p_i^* - p_j^*$ .  $d_{min}$  is the minimum distance between all robot manipulators for obstacle avoidance. The safety distance  $d_0$  is a positive constant resolved by the developer.

Conventionally, the basic strategy for obstacle avoidance is to identify the  
 155 points on the robotic arm that are near obstacles and then assign to them the motion component that moves those points away from the obstacle, as shown in Fig. 1. The robot motion (configuration) is changed if at least one part of the



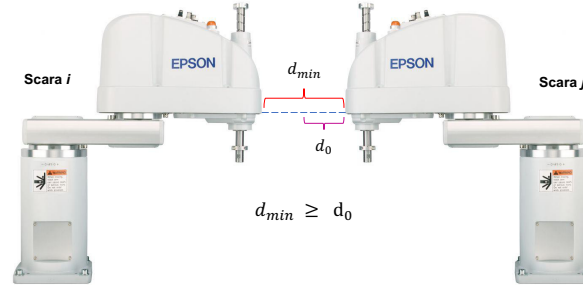


Figure 1: Two SCARA robots moving towards each other while avoiding collision.  $d_{min}$  is the minimum distance between the two robots. For safety consideration,  $d_{min} \geq d_0$ , where  $d_0$  is the critical distance.

robot is at a critical distance from an obstacle. We denote the obstacles that are closer to the critical distance as the active obstacles and the corresponding  
 160 closest points on the body of the manipulator as the critical points.

**Remark 1.** For industrial robots it is usually assumed that the motion of the end-effector is not disturbed by any obstacle. If such a situation occurs, either the task execution has to be interrupted and the higher-level path planning has to recalculate the desired motion of the end-effector.

### 165 2.3. Control Objective

In this paper, we consider **obstacle avoidance** problem of multi-robot collaboration for multiple planar non-redundant robot manipulators, where precise values of kinematic parameters are **available**. Based on this target, we proposed the safety precaution mechanism. In order for us to achieve this goal, we adjust  
 170 this kinematic control problem to an optimization problem in which obstacle avoidance condition **turns into** an inequality constraint of the optimization problem. More specifically, we keep this avoidance constraint always fulfilled, while trying to make end-effector's kinematic error as small as possible.

The control objective, theoretically speaking, is to express  $d_{min}$  in the inequality constraint, and with the aid of our RNN algorithm as the main tool  
 175

for solution, we can manage to find the minimum value of the optimization problem which is down to the joint velocity level to find the norm distance of critical points of joints' actual speed  $\dot{p}_i^*$  to the end-effectors' desired speed  $\dot{r}_{id}$ . As mentioned earlier,  $d_{min}$  is the minimum distance between all robot manipulators for obstacle avoidance. However, how to find  $d_{min}$  and keep the condition  $d_{min} \geq d_0$  remain the biggest challenge for this research experiment.

### 3. Quadratic Problem Formulation

#### 3.1. Original QP Formulation

Based on above mentioned, the kinematic control of a redundant manipulator while avoiding obstacles can be prudently described as:

$$\min \sum_{i=1}^N \|r_i(t) - r_{id}(t)\|^2/2, \quad (4a)$$

$$s.t. \quad r_i(t) = f(\theta_i(t)), \quad i = 1, \dots, N, \quad (4b)$$

where  $r_i(t)$  and  $r_{id}(t)$  are the actual position and desired position of end-effector respectively;  $p_i^*, p_j^*$  are the critical points resulting minimum distance  $d_{min}$ , i.e.  $d_{min} = \|p_i^* - p_j^*\|$ .

As seen from (4), the end-effector of the manipulator is expected to track a desired path defined by  $r_d(t)$ , which is often referred to as the primary task of a manipulator. Specifically, during the tracking process, the position norm  $r_i(t) - r_{id}(t)$  needs to be minimized.

#### 3.2. QP Reformulation

Directly finding the direct solution for (4) is quite difficult, we need to make some adjustments if we want to receive an expressive answer. The main reason behind this phenomenon is that all three formulas were made in the displacement(position) level, which is not quite related to our control quality  $\dot{\theta}$ . Therefore, to bypass this barrier, the best way to go about it is to reformulate these

equations to which can link to  $\dot{\theta}$  directly, so that they can facilitate the progress  
 200 of our research.

The **derivation** process can be presented as to focus on transforming the original optimization function, and from there branch out new twigs of original inequality constraint, and arrive at the ultimate version of our constrained optimization problem formulation.

205 For a non-redundant manipulator described by Equation(2) that is subject to the joint velocity  $\dot{\theta}(t)$ , we wish to find a control variable  $\dot{\theta}(t)$ , such that the tracking error  $e_i(t) = r_i(t) - r_{id}(t)$  for a given reference trajectory  $r_{id}(t)$  converges over time. Generating joint velocity  $\dot{\theta}(t)$  command in real-time to ensure the difference between  $r_i(t) - r_{id}(t)$  converges to zero.

210 By using the formula  $\dot{e}(t) = -C_0 e(t)$ , which guarantees that  $e(t)$  exponentially converges to zero with constant  $C_0 > 0 \in \mathbb{R}$  being the parameter to scale the convergence rate, the following equation is obtained:

$$\dot{r}_{iref}(t) = \dot{r}_{id}(t) - C_0(r_i(t) - r_{id}(t)), \quad (5)$$

From (4) and (5), the objective function can be rewritten as follows:

$$\min \sum_{i=1}^N \|r_i(t) - r_{iRef}(t)\|^2/2. \quad (6)$$

Based on  $d_{min} = \|p_i^* - p_j^*\|$ , we can consider  $p_i^*, p_j^*$  at the velocity level, which equal  $\dot{p}_i^*, \dot{p}_j^*$ . We can further rewrite the formula for the inequality constraint as following:

$$\begin{aligned} d_{min} \geq d_0 &\Leftrightarrow \|p_i^* - p_j^*\|^2/2 \geq d_0^2/2, \\ (p_i^* - p_j^*)^T (p_i^* - p_j^*) &\geq -k_1[d_{min}^2/2 - d_0^2/2] \end{aligned} \quad (7)$$

By algebraically rewriting, we have

$$(p_i^* - p_j^*)^T (J_i^* \dot{\theta}_i^* - J_j^* \dot{\theta}_j^*) \geq -k_1[d_{min}^2/2 - d_0^2/2], \quad (8)$$

with  $k_1 > 0$  is used to adjust the tracking accuracy of the manipulator to the

desired trajectory, and then we define  $a_1, a_2, a_3$  to be the value of:

$$\begin{aligned} a_1 &\equiv -(p_i^* - p_j^*)^T J_i^*, \\ a_2 &\equiv (p_i^* - p_j^*)^T J_j^*, \\ a_3 &\equiv -k_1[d_{min}^2/2 - d_0^2/2]. \end{aligned}$$

From Equation (8), we have the following format:

$$a_1\dot{\theta}_i^* + a_2\dot{\theta}_j^* + a_3 \leq 0. \quad (9)$$

Refer back to (2),  $\dot{\theta}_i$  is the angular speed of a specific joint of the manipulator,  $J_i$  is the Jacobian matrix from the critical point to joint space. Then the velocities of critical points can be described as  $\dot{r}_i = J_i\dot{\theta}_i^*$ .

Hence, we have the new form of constrained optimization problem:

$$\min \|J_i\dot{\theta}_i^* - \dot{r}_{iRef}\|^2/2, \quad (10a)$$

$$s.t. a_1\dot{\theta}_i^* + a_2\dot{\theta}_j^* + a_3 \leq 0. \quad (10b)$$

#### 4. Design of Recurrent Neural Network

As stated in Section I, the kinematic control of non-redundant manipulators using RNNs has been extensively studied in recent decades. Although the existing methods of this type differ in the objective functions or neural dynamics used, most of them follow similar design principles. The redundant manipulator control problem is typically formulated as a constrained quadratic optimization problem, which can be equivalently converted into a set of implicit equations. Then, a convergent RNN model, the equilibrium of which is identical to the solution of this implicit equation set, is devised to solve the problem recursively.

In this paper, the secondary task is set to minimize joint velocity while avoiding obstacles. In real implementations, both joint angles and velocities are limited because of physical limitations such as mechanical constraints and actuator saturation. In this paper, we aim to design a kinematic controller which is capable of avoiding obstacles while tracking a pre-defined trajectory

in the cartesian space. For safety's sake, the robot is wished to move at a low speed, on the other hand, lower energy consumption is guaranteed.

#### 4.1. Setup Lagrange Function

Consider a Lagrange function as

$$L = \sum_{i=1}^n (J_i \dot{\theta}_i - \dot{r}_{iRef})^T (J_i \dot{\theta}_i - \dot{r}_{iRef}) / 2 + u(a_1 \dot{\theta}_i^* + a_2 \dot{\theta}_j^* + a_3), u \in \mathbb{R}^m \quad (11)$$

235 with  $u$  serves as the Lagrange multiplier corresponding to the inequality constraint (10).

#### 4.2. KKT Condition

According to Karush-Kuhn-Tucker conditions, the optimal solution of the optimization problem (11) can be equivalently formulated as:

$$\frac{\partial L}{\partial \theta_i(t)} = 0 \quad (12a)$$

$$(u + a_1 \dot{\theta}_i^* + a_2 \dot{\theta}_j^* + a_3)^+ = u \quad (12b)$$

Which can be elaborated as:

$$J_i^T (J_i \dot{\theta}_i - \dot{r}_{iRef}) + a_2^T u = 0, \text{ for robot } i \quad (13a)$$

$$J_j^T (J_j \dot{\theta}_j - \dot{r}_{jRef}) + a_1^T u = 0, \text{ for other robot} \quad (13b)$$

$$(u + a_1 \dot{\theta}_i^* + a_2 \dot{\theta}_j^* + a_3)^+ = u \quad (13c)$$

240 In Equation (12b) and (13c), the operation function  $(\cdot)^+$  is defined as a mapping to the non-negative space. For instance,  $x^+ = \max(x, 0)$  takes the positive part of the real  $x$ , denoted by  $x^+$ .

#### 4.3. RNN design

245 The solution of (13) is exact optimal solution of the constrained-optimization problem (10), it is still a challenging issue to solve (13) online since its inherent

nonlinearity. In this paper, in order to solve (13), a recurrent neural network is designed as:

$$\ddot{\theta}(t) = -k_0[J_i^T(J_i\dot{\theta}_i - \dot{r}_{iRef}) + a_1^T u], \quad (14a)$$

$$\ddot{\theta}(t) = -k_0[J_j^T(J_j\dot{\theta}_j - \dot{r}_{jRef}) + a_2^T u], \quad (14b)$$

$$\dot{u} = k_0[(u + a_1\dot{\theta}_i^* + a_2\dot{\theta}_j^* + a_3)^+ - u]. \quad (14c)$$

where  $k_0 > 0$  is a constant which is used to scale the convergence rate of neural network.  $\lambda = 0$  will always hold for  $d_{min} = \|p_i^* - p_j^*\| \geq d_0$ , except when the collision detection mechanism is met, (14c) comes into play. Now,  $\lambda > 0$ .

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**Algorithm 1** Multiple SCARAs cooperation incorporated with obstacle avoidance based on RNN

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**Input:** Control parameters  $\varepsilon, k_1$ , number of SCARAs  $n$ ; SCARA parameters  $r_d, L, d_0$ ; task duration and internal  $t_s, d_t$ , safety distance  $d_0$ ; initial parameters  $\theta_i(0), \dot{\theta}_i(0)$ , base; desired trajectory information  $r_{id}$  and  $\dot{r}_{id}$ ; feedback information  $r_{iRef}$  and  $\dot{r}_{iRef}$ .

**Output:** To simultaneously achieve obstacle avoidance and global cooperation between multiple SCARAs.

- 1: **while**  $t < t_s$  **do**
  - 2: Reading  $\dot{r}_{iRef}, \theta(t)$  by sensor.
  - 3: Calculate  $\dot{r}_{iRef}$  and error  $e = r_{id} - r_{iRef}$ .
  - 4: Calculate  $A, B$ .
  - 5: Update joint velocities of every SCARA using Eq.(26a).
  - 6: Update state variable  $\lambda$  using Eq.(26b).
  - 7: Update  $\theta$  and  $r_{iRef}$ .
  - 8: **end while**
- 

#### 4.4. Optimality and Convergence Analysis

In this subsection, we provide stability and convergence analysis of the obstacle avoidance algorithm based on sophisticated RNN method to show our

controller can reach an optimal solution through iterations of feedback distance  
 255 tracking. The theoretical derivation process [relies](#) on important definitions and  
 lemmas.

**Definition 1 (Projection Operator).** The projection operator for a set  $S \subset \mathbb{R}^m$  and  $x \in S$  is defined by:

$$P_S(x) = \operatorname{argmin}_{y \in S} \|y - x\|^2, \quad (15)$$

where  $\|\cdot\|$  denotes the Euclidean norm.

260 **Definition 2 (Monotone Mapping).** A mapping  $F(\cdot)$  is called monotone if  
 for each pair of points  $(x, y)$ , there is:

$$(x - y)^T (F(x) - F(y)) \geq 0. \quad (16)$$

This property can be [extended](#) to multi-variable mappings. For a continuously  
 differentiable mapping  $F(\cdot)$ , it is a monotone mapping if

$$\nabla F + \nabla^T F \geq 0, \quad (17)$$

where ' $\geq 0$ ' means the left side of this operator is positive semi-definite, knowing  
 $\nabla F$  is the gradient of  $F(\cdot)$ .

**Lemma 1 (Convergence Of Dynamic Neural Networks).** Assume that  
 265  $F(x)$  is monotone and continuously differentiable. The dynamic system (18)  
 is said to [converge](#) to its equilibrium point correspond to:

$$k\dot{x} = -x + P_s(x - \varrho F(x)), \quad (18)$$

where  $k > 0$  and  $\varrho > 0$  are both positive constants. (15) is a projection operator  
 to closed set  $S$ .

*Proof:* There are two parts of analysis: Part I is to reformulate the designed  
 270 RNN (14) as the form of (18). Part II is to compute the value of the expression  
 shown in (17).

*Part I:* First provide value ranges of three parameters, assuming there are  $N$  robots in the environment, let

$$r_i = \begin{bmatrix} r_1 \\ r_2 \\ \vdots \\ r_N \end{bmatrix} \in \mathbb{R}^{2N}, r_{id} = \begin{bmatrix} r_{1d} \\ r_{2d} \\ \vdots \\ r_{Nd} \end{bmatrix} \in \mathbb{R}^{2N} \quad (19)$$

$$\theta_i = \begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_N \end{bmatrix} \in \mathbb{R}^{2N}. \quad (20)$$

by rewriting (8) as  $H\dot{\theta} \leq H_R$ , where  $H$  is  $-(p_i^* - p_j^*)^T(J_i - J_j)$  and  $H_R$  is  $k(\|r_i - r_j\|^2/2 - d_0^2/2)$ . From (10) We have:

$$\min \|r_i - r_{iRef}\|^2/2, \quad (21a)$$

$$s.t. H\dot{\theta} \leq H_R. \quad (21b)$$

To elaborate on 21b,  $H = -ABC$ . Matrix  $A = \text{diag}(M) \in \mathbb{R}^{(N^2-N)/2 \times (N^2-N)}$  with  $M = [m_{12}, m_{13}, \dots, m_{ij}, \dots, m_{(N-1)N}] \in \mathbb{R}^{1 \times 2N}$ .  $\text{diag}(\bullet)$  denotes a diagonal matrix and  $m_{ij}$  is represented as  $m_{ij} = (p_i^* - p_j^*)^T, i = 1, \dots, N-1; j = i+1, \dots, N$ . The complete form of  $A$  is displayed below:

$$A = \begin{bmatrix} (p_1^* - p_2^*)^T & & & & \\ & (p_1^* - p_3^*)^T & & & \\ & & \ddots & & \\ & & & \ddots & \\ & & & & (p_{N-1}^* - p_N^*)^T \end{bmatrix} \in \mathbb{R}^{(N^2-N)/2 \times (N^2-N)}, \quad (22)$$

Additionally,  $B$  and  $C$  are expressed in the following:

$$B = \begin{bmatrix} I & -I & 0 \\ I & 0 & -I \\ 0 & I & -I \end{bmatrix} \in \mathbb{R}^{(N^2-N) \times 2N}, \quad (23)$$



$$C = \begin{bmatrix} J_1 & & & \\ & J_1 & & \\ & & \ddots & \\ & & & J_N \end{bmatrix} \in \mathbb{R}^{2N \times 2N}. \quad (24)$$

The Lagrange function and its derivative are compute as followed:

$$L = \|r_i - r_{iRef}\|^2/2 + \lambda^T(H\dot{\theta} - H_R), \quad (25a)$$

$$\frac{\partial L}{\partial \dot{\theta}} = J^T(\dot{r} - \dot{r}_{iRef}) + H^T\lambda. \quad (25b)$$

The designed RNN(14) becomes:

$$\begin{aligned} k\ddot{\theta} &= -\dot{\theta} + P_\Omega(\dot{\theta} - \frac{\partial L}{\partial \dot{\theta}}) \\ &= -\dot{\theta} + P_\Omega(\dot{\theta} - J^T(J\dot{\theta} - \dot{r}_{iRef}) - H^T\lambda), \end{aligned} \quad (26a)$$

$$k\dot{\lambda} = -\lambda + (\lambda + H\dot{\theta} - H_R)^+. \quad (26b)$$

*Part II:* Define  $x = [\dot{\theta} ; \lambda]$ , so that (26) can be [converted](#) to:

$$F(x) = \begin{bmatrix} J^T(J\dot{\theta} - \dot{r}_{iRef}) + H^T\lambda \\ -H\dot{\theta} + H_R \end{bmatrix}.$$

From (17), we have:

$$\nabla F(x) = \begin{bmatrix} J^T J & H^T \\ -H & 0 \end{bmatrix},$$

and

$$(\nabla)^T F(x) = \begin{bmatrix} J^T J & -H \\ H^T & 0 \end{bmatrix}.$$

Thus,  $F(x)$  is continuously differentiable in light of the existence of  $\nabla F(x)$ ; furthermore, we can [sum](#) them together to produce:

$$\nabla F(x) + (\nabla)^T F(x) = \begin{bmatrix} 2J^T J & 0 \\ 0 & 0 \end{bmatrix}.$$

275 According to Definition 2, we can conclude that  $\nabla F(x) + (\nabla)^T F(x)$  is indeed positive semi-definite, and  $F(x)$  is monotone function.

From Lemma 1, it can be summarized from the above analyses with generalized description that the proposed dynamical neural network(14) is stable and is globally convergent to the optimal solution of (10). The proof is completed.

## 280 5. Numerical Results

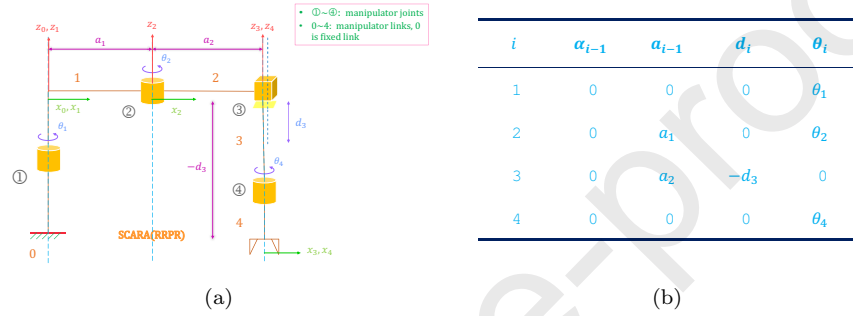


Figure 2: Scara manipulator kinematic properties. (a) Analysis of Scara's physical structure. (b) D-H parameters of Scara manipulator.

In this section, the proposed RNN based controller is applied to three planar 2-link robots. Fig. 2 is a detailed self-explanatory supplement to our agenda. Complying to the principle of our main task, a simplified yet sufficient version of the Scara robot—2-link planar non-redundant type of Scara robot is going to be the main object that we studied in this experiment. Firstly, a successful case where manipulators are allowed to draw circles by pre-defined trajectory planning is discussed, and then the controller is tested to run with the case that manipulators follow the safety protocol which cannot finish the task because of obstacles avoidance mechanism.

### 290 5.1. Simulation Setup

To verify the effectiveness of our controller, we decide to implement our simulation on three Scara manipulators for validation. The general physical structure of the 2-link Scara manipulator can be dissected as shown in Figure. 2(a). The Kinematic characteristics are also displayed in Figure. 2(b). It is

295 noteworthy to point out that Jacobian matrix  $J_2$ , critical points coordinates  $P_i$ ,  
 manipulators' angular speed and end-effectors' coordinates are the key variables  
 in the proposed [control](#) scheme.

For our simulation, the 3D model of Scara manipulator in Figure. 3. marked  
 with critical points  $P_1, P_2$  and  $P_3$  is more intuitive for inspection and compre-  
 300 hension. As shown in Figure. 3, critical points  $P_1, P_2$  and  $P_3$  are selected at the  
 center of manipulators' joints.

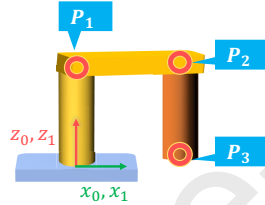


Figure 3: 3D model of Scara manipulator

Based on the above description of Scara manipulators, for the sake of this  
 research experiment, we establish the following parameters: The values of the  
 number of manipulators  $n$ , manipulators' link length  $L$ , manipulators' base co-  
 305 ordinates  $base$ , manipulators' initial joints' angle  $\theta$ , manipulators' initial joints'  
 angular speed  $\dot{\theta}$ , and manipulators' end-effectors' initial coordinates  $r_d$  are all  
 known at the start of this experiment.

Since the goal of controlled simulation is to the express  $d_{min}$  such that  
 $d_{min} \geq d_0$  is fulfilled, our focus next is to express this inequality constraint as the  
 310 relationship between critical points of the manipulator. Therefore, to find the  
 norm of the distance between the critical point of a manipulator  $p_1^*$  and another  
 critical point of second manipulator  $p_2^*$  is the next step, i.e.  $d_{min} = \|p_1^* - p_2^*\|$ .  
 After the long inequality constraint is formed as Equation(12) shown, we use  
 $a_1, a_2, a_3$  to denote three polynomials as parts of the Equation(13), and we  
 315 realize these formulas in the core body of the RNN algorithm code. Finally, the

optimization index  $\mu$  is achieved and updated as simulation proceed.

## 5.2. Simulation Results

The RNN controller is comprised of two parts: motion tracking and collision avoidance. When robots run in a collision-free environment, motion tracking  
 320 plays the dominant role; however, as collision is detected, the obstacle avoidance mechanism takes control.

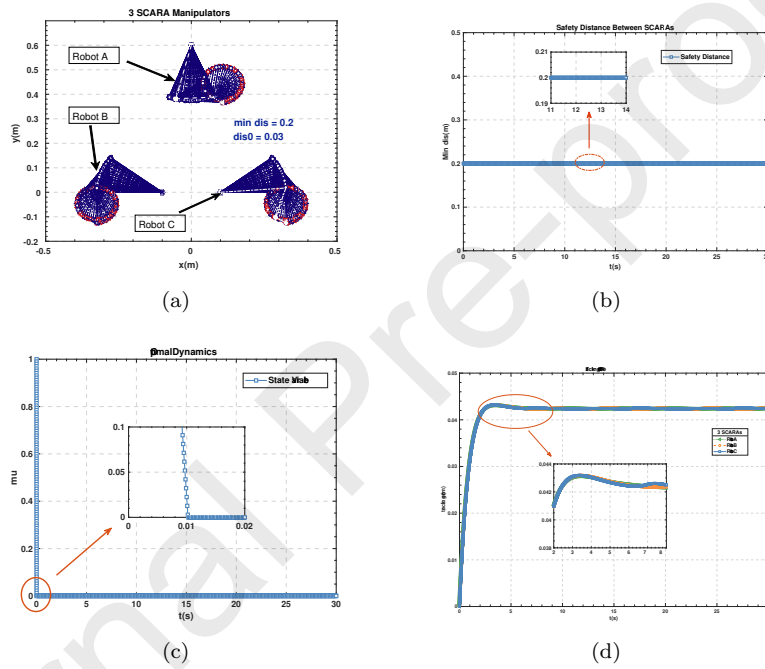


Figure 4: Simulation results for the kinematic control of end effector of three 2-link Scara robots where each of them is placed to be interference-free from other robots along a circular path. (a) End-effector trajectory (blue curves) with respect to the reference position. (b) Minimum distance determined by RNN algorithm to maintain safety between robots. (c) Ensuring the inequality constraint (10b), Optimized index( $\mu$ ) is measured at  $k_0 = 10^5$ . (d) Tracking errors with respect to time history at  $k_0 = 10^5$ .

### 5.2.1. Obstacle Free

As indicated in Fig. 4, from plot (a) can readily see the harmonious working environment between the three 2-link planar Scara robots. One robot is located

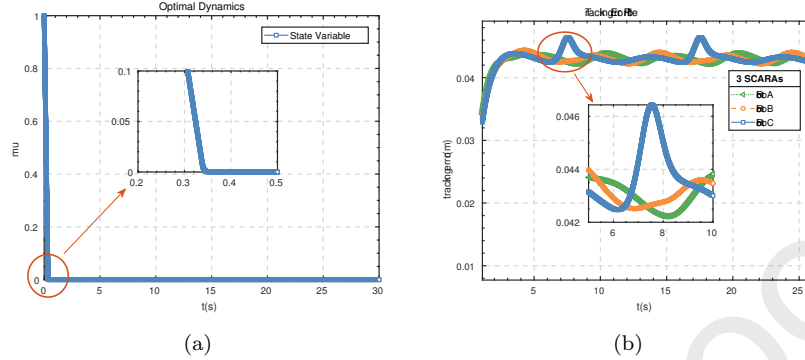


Figure 5: Simulation results for the kinematic control of end effector of three 2-link Scara robots where each of them is placed to be interference-free from other robots along a circular path. It is remarkable to note that  $k_0 = 10^3$  achieves slower convergence of  $\mu$ , thus The larger  $k_0$ , the faster the RNN converges. (a) Optimized index(smaller  $k_0$ ). (b) Obstacle-free tracking errors

325 on top of the figure, and the other two robots are based on the middle part of  
 figure, all of them are placed on the same platform. In this case, we select  $dis_0 =$   
 $0.03$  to be the value for safety distance, and the instant value for  $min\ dis$  after  
 the simulation finished is  $0.2$ . The state variable also named as the optimization  
 index  $u$  is put into the control scheme so that the inequality constraint (10b)  
 330 is ensured, as shown in (13c) and also in the code where the kernel of RNN  
 is placed. The Index  $u$  is updated according to the difference between actual  
 speed  $J_i\dot{\theta}_i^*$  and reference speed  $\dot{r}_{iRef}$ . During the experiment, it is engaging to  
 find out that  $k_0$  plays an significant role in the convergence of the RNN control  
 system. The larger  $k_0$ , the faster the RNN converges. From Fig. 4(c) and (d),  
 335 the simulation performance result can verify our initial statement which is this  
 simulation is successfully ran. The zoom-in figure within Fig. 4(d) exhibits the  
 process is carried smoothly and congruently, indicating no collision risk. From  
 Fig. 5(a) and (b), an illustration of the optimized controller converges in a  
 slower response.

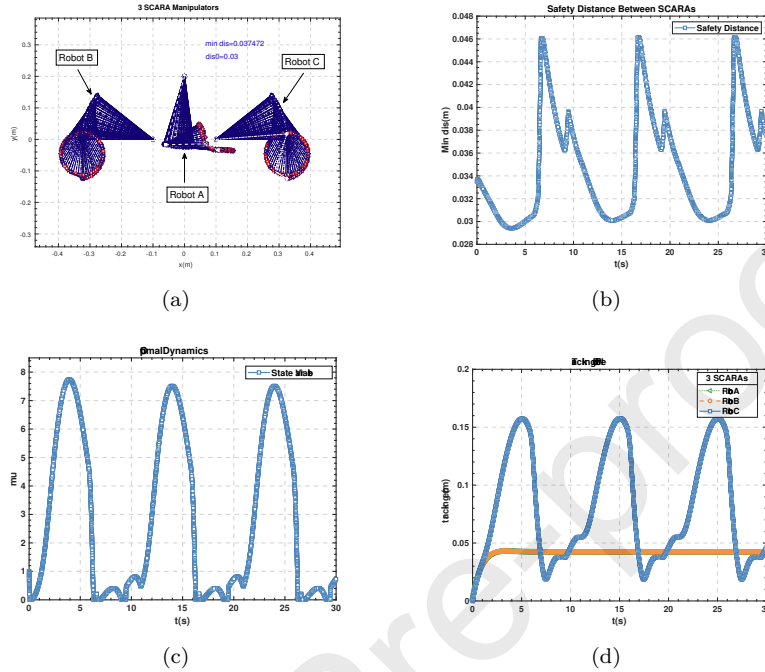


Figure 6: Simulation results for the kinematic control of end effector of three 2-link Scara robots where each of them is placed to have interference(obstacle detected) from other robots along a circular path. (a) End-effector trajectory (blue curve) with respect to the reference position. (b) Minimum distance determined by RNN algorithm to maintain safety between robots. (c) Ensuring the inequality constraint (10b), Optimized index( $\mu$ ) is measured at  $k_0 = 10^5$ . (d) Tracking errors with respect to time history at  $k_0 = 10^5$ .

### 340 5.2.2. Obstacle Encountered

In this scenario, an illustration of the case when the middle Scara robots strived for trajectory tracking as its original kinematic motion object, but as displayed that the middle robot is continuously moving in its best to approach the pre-defined curve, this is under the influence of the safety precaution implanted  
 345 to prevent robots from running too close to collide with each other. We can also comprehend this as Fig. 6(a) and 6(d) shown, both plots indicate that the middle robot tried to avoid running into the robot on the right during simulation. In Fig. 6(d), both the left and right robots are running ordinarily

with planned trajectories, however the middle robot is following safety protocol  
 350 to avoid collision, this is the reason that the purple line deviates from other  
 two tracking errors. Based on this phenomenon, an conclusion can be summed  
 up: 1) Avoid placing robots too close to one another. 2) The safety distance  
 can affect the simulation as it can pose a hedge while robots are in operation.  
 3) Slow down the angular speed of end-effectors can support the movement  
 355 realization as to give more time for robots to react with incoming obstacles.

## 6. Conclusion

In allusion to obstacles avoidance between operational robots among multi-  
 robot collaboration, this paper represents the knowledge of Recurrent Neural  
 Network method specialized designed for preventing collisions between robot  
 360 manipulators, and proposes a corresponding mechanism of safety assurance  
 based on a unique control constraint that can trigger the precautions when  
 certain parts of machines are determined to be within the safe distance. Utiliz-  
 ing geometric features of manipulators, the manipulators can be denoted by sets  
 of critical points, thereby the distance between the robots is approximately de-  
 365 scribed as point-to-points distances. Therefore, the collision avoidance strategy  
 can be formulated as an inequality constraints. By keeping the minimal distance  
 between robots, collision-free environment is ensured. With three Scara robots,  
 we perform simulative experiments on Matlab, indicating that when the mini-  
 mal distance between robots is less than the setting safety distance, the collision  
 370 avoidance strategy come in the control command, the robots successfully avoid  
 collision with other manipulators. If forthcoming path is free of obstacles, the  
 robot performs the desired trajectory tracking task with a promising tracking  
 error. In the future, this proposed method can be further upgraded to apply for  
 multiple redundant industrial manipulators in three-dimensional space. Each  
 375 robot act as a player in the game theory, and by having an inequality con-  
 trol constraint which treats all other robots as obstacles, a congruous industrial  
 multi-robot collaboration platform can be achieved.

**References**

- [1] T. Arai, E. Pagello, L. E. Parker, et al., Advances in multi-robot systems, *IEEE Transactions on robotics and automation* 18 (5) (2002) 655–661. 380
- [2] W. Burgard, M. Moors, C. Stachniss, F. E. Schneider, Coordinated multi-robot exploration, *IEEE Transactions on robotics* 21 (3) (2005) 376–386.
- [3] B. Yamauchi, Frontier-based exploration using multiple robots, in: *Proceedings of the second international conference on Autonomous agents*, 1998, pp. 47–53. 385
- [4] R. Kurazume, S. Nagata, S. Hirose, Cooperative positioning with multiple robots, in: *Proceedings of the 1994 IEEE International Conference on Robotics and Automation*, IEEE, 1994, pp. 1250–1257.
- [5] T. Petrič, A. Gams, N. Likar, L. Žlajpah, Obstacle avoidance with industrial robots, in: *Motion and Operation Planning of Robotic Systems*, Springer, 2015, pp. 113–145. 390
- [6] H. Lee, H. Kim, H. J. Kim, Path planning and control of multiple aerial manipulators for a cooperative transportation, in: *2015 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, IEEE, 2015, pp. 2386–2391. 395
- [7] W. F. Carriker, P. K. Khosla, B. H. Krogh, Path planning for mobile manipulators for multiple task execution, *IEEE Transactions on Robotics and Automation* 7 (3) (1991) 403–408.
- [8] X. Li, J. Xiao, Z. Cai, Backstepping based multiple mobile robots formation control, in: *2005 IEEE/RSJ International Conference on Intelligent Robots and Systems*, IEEE, 2005, pp. 887–892. 400
- [9] C. Cai, C. Yang, Q. Zhu, Y. Liang, Collision avoidance in multi-robot systems, in: *2007 International Conference on Mechatronics and Automation*, IEEE, 2007, pp. 2795–2800.



- 405 [10] D. P. Garg, M. Kumar, Optimization techniques applied to multiple manipulators for path planning and torque minimization, *Engineering applications of artificial intelligence* 15 (3-4) (2002) 241–252.
- [11] Y. Zhang, J. Wang, Obstacle avoidance of redundant manipulators using a dual neural network, in: *2003 IEEE International Conference on Robotics and Automation* (Cat. No. 03CH37422), Vol. 2, IEEE, 2003, pp. 2747–2752.
- 410 [12] Y. Zhang, J. Wang, Obstacle avoidance for kinematically redundant manipulators using a dual neural network, *IEEE Transactions on Systems, Man, and Cybernetics, Part B (Cybernetics)* 34 (1) (2004) 752–759.
- [13] Z. Xu, X. Zhou, S. Li, Deep recurrent neural networks based obstacle avoidance control for redundant manipulators, *Frontiers in neurorobotics* 13 (2019) 47.
- 415 [14] A. H. Khan, S. Li, X. Luo, Obstacle avoidance and tracking control of redundant robotic manipulator: An rnn based metaheuristic approach, *IEEE Transactions on Industrial Informatics*.
- [15] G. Li, Q. Jia, Cooperative receding horizon path planning of multiple robots by genetic algorithm, in: *2008 IEEE International Conference on Automation and Logistics*, IEEE, 2008, pp. 2449–2453.
- 420 [16] S. Sun, A. S. Morris, A. M. Zalzal, Trajectory planning of multiple coordinating robots using genetic algorithms, *Robotica* 14 (2) (1996) 227–234.
- [17] G. Peng, C. Yang, W. He, C. P. Chen, Force sensorless admittance control with neural learning for robots with actuator saturation, *IEEE Transactions on Industrial Electronics* 67 (4) (2020) 3138–3148.
- 425 [18] H. Huang, T. Zhang, C. Yang, C. P. Chen, Motor learning and generalization using broad learning adaptive neural control, *IEEE Transactions on Industrial Electronics* 67 (10) (2020) 8608–8617.
- 430

- [19] C. Yang, C. Chen, W. He, R. Cui, Z. Li, Robot learning system based on adaptive neural control and dynamic movement primitives, *IEEE transactions on neural networks and learning systems* 30 (3) (2019) 777–787.
- [20] Y. Yamamoto, S. Fukuda, Trajectory planning of multiple mobile manipulators with collision avoidance capability, in: *Proceedings 2002 IEEE International Conference on Robotics and Automation (Cat. No. 02CH37292)*, Vol. 4, IEEE, 2002, pp. 3565–3570.
- [21] J. Wang, X. Ren, J. Liu, Trajectory planning for multi-robot formation by one hybrid particle swarm optimization algorithm, in: *2013 5th International Conference on Intelligent Human-Machine Systems and Cybernetics*, Vol. 1, IEEE, 2013, pp. 344–348.
- [22] A. Mohri, M. Yamamoto, G. Hirano, Cooperative path planning for two manipulators, in: *Proceedings of IEEE International Conference on Robotics and Automation*, Vol. 3, IEEE, 1996, pp. 2853–2858.
- [23] F. Lewis, S. Jagannathan, A. Yesildirak, *Neural network control of robot manipulators and non-linear systems*, CRC Press, 1998.
- [24] G. Wittenberg, Developments in offline programming: an overview, *Industrial Robot: An International Journal* 22 (3) (1995) 21–23.
- [25] Z. Pan, J. Polden, N. Larkin, S. Van Duin, J. Norrish, Recent progress on programming methods for industrial robots, in: *ISR 2010 (41st International Symposium on Robotics) and ROBOTIK 2010 (6th German Conference on Robotics)*, VDE, 2010, pp. 1–8.
- [26] C. Kohrt, R. Stamp, A. Pipe, J. Kiely, G. Schiedermeier, An online robot trajectory planning and programming support system for industrial use, *Robotics and Computer-Integrated Manufacturing* 29 (1) (2013) 71–79.
- [27] F. L. Lewis, D. Liu, *Reinforcement learning and approximate dynamic programming for feedback control*, Vol. 17, John Wiley & Sons, 2013.

- [28] A. Nagabandi, G. Kahn, R. S. Fearing, S. Levine, Neural network dynamics for model-based deep reinforcement learning with model-free fine-tuning, in: 2018 IEEE International Conference on Robotics and Automation (ICRA), IEEE, 2018, pp. 7559–7566.
- [29] J. Botzheim, Y. Toda, N. Kubota, Bacterial memetic algorithm for offline path planning of mobile robots, *Memetic Computing* 4 (1) (2012) 73–86.
- [30] S. Lin, A. A. Goldenberg, Neural-network control of mobile manipulators, *IEEE Transactions on Neural networks* 12 (5) (2001) 1121–1133.
- [31] Y. H. Kim, F. L. Lewis, Neural network output feedback control of robot manipulators, *IEEE Transactions on robotics and automation* 15 (2) (1999) 301–309.
- [32] R. W. Parks, D. L. Long, D. S. Levine, D. J. Crockett, E. G. McGeer, P. L. McGeer, I. E. Dalton, R. F. Zec, R. E. Becker, K. L. Coburn, et al., Parallel distributed processing and neural networks: Origins, methodology and cognitive functions, *International journal of neuroscience* 60 (3-4) (1991) 195–214.
- [33] L. Jin, S. Li, J. Yu, J. He, Robot manipulator control using neural networks: A survey, *Neurocomputing* 285 (2018) 23–34.
- [34] W. He, Y. Chen, Z. Yin, Adaptive neural network control of an uncertain robot with full-state constraints, *IEEE transactions on cybernetics* 46 (3) (2015) 620–629.
- [35] B. Jin, Robotic manipulator trajectory control using neural networks, in: *Proceedings of 1993 International Conference on Neural Networks (IJCNN-93-Nagoya, Japan)*, Vol. 2, IEEE, 1993, pp. 1793–1796.
- [36] N. Bin, C. Xiong, Z. Liming, X. Wendong, Recurrent neural network for robot path planning, in: *International Conference on Parallel and Distributed Computing: Applications and Technologies*, Springer, 2004, pp. 188–191.

- [37] W. S. Tang, C. M. L. Lam, J. Wang, Kinematic control and obstacle avoidance for redundant manipulators using a recurrent neural network, in: International Conference on Artificial Neural Networks, Springer, 2001, pp. 922–929.
- <sup>490</sup> [38] H. Ding, J. Wang, Recurrent neural networks for minimum infinity-norm kinematic control of redundant manipulators, IEEE Transactions on Systems, Man, and Cybernetics-Part A: Systems and Humans 29 (3) (1999) 269–276.