

1           **Modelling the morphodynamic evolution of Galveston beach, Gulf of**  
2   **Mexico, following Hurricane Ike in 2008**

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11  
12   **Abstract**

13   A unique set of field measurements taken along Galveston beach have been compiled to give  
14   annual shoreline positions over the period 2010-2016. These have been used, in conjunction  
15   with statistical and mathematical modelling, to gain insights into the response of the shoreline  
16   after the landfall of Hurricane Ike in 2008, which caused extensive erosion and loss of  
17   material from the beach. Over the period 2010-2014, a generally accretive trend is observed  
18   along the beach. Within this trend, two different patterns are evident. In the area extending  
19   westward of South Jetty the accretion rate is fast until April 2011, after which the accretion  
20   rate decreases. The remainder of the beach, including the groyne field in front of the city of  
21   Galveston, exhibits the greatest accretive trend after April 2011. It is hypothesised that  
22   distinct sandbanks lying offshore of Galveston Island were formed during the passage of  
23   Hurricane Ike and control these two different patterns of recovery. To test this hypothesis a  
24   novel 1-line model, based on linked analytical solutions, was set up to investigate the beach  
25   response to various sediment source distributions. The model was tested against existing

26 survey measurements and performed satisfactorily. An exploration of various sediment  
27 supply scenarios with the model supports the hypothesis that offshore sediment stores, one  
28 distinct source to the south of South Jetty and a diffuse linear source running the length of the  
29 groyne field and seawall, were gradually being fed back to the beach by the prevailing wave  
30 conditions.

31 **Keywords:** groyne-field, shoreline evolution, accretion, One-Line model, Galveston beach,  
32 Hurricane Ike, semi-analytical solution

33

## 34 **1. Introduction**

### 35 **1.1. Background**

36 Galveston Island is a sandy barrier island system near Houston in the Gulf of Mexico that  
37 extends *44 km* alongside the mainland, from Bolivar Roads to San Luis Pass (Fig. 1). A  
38 unique set of shoreline surveys has provided the basis for an exploration of the recovery of  
39 Galveston beach after the passage of Hurricane Ike. These, combined with a semi-analytical  
40 one-line model, have been used to gain insights into the meso-scale recovery process of the  
41 beach. An explanation of the morphodynamic evolution of a section of Galveston beach near  
42 Galveston city extending approximately 17km westwards from South Jetty is proposed, as a  
43 result.

44 Shoreline changes and sediment budgets in this area are affected by natural processes. Two  
45 inlets, namely Bolivar Roads and San Luis Pass, and engineered coastal structures including  
46 jetties, the Galveston seawall, and an associated groyne field in front of the seawall act to  
47 control the sediment movement along the shore. Bolivar Roads is the main ship channel  
48 connecting the Gulf of Mexico and Galveston Bay enabling ship traffic in and out of several  
49 major harbours (Houston, Galveston, Texas City). The shipping lane is maintained to a depth  
50 of *14 m* and is protected by jetties on either side. The north and south jetties extend *7.6* and

51 3.9 km, respectively, from the shoreline. San Luis Pass is an inlet not maintained by dredging  
52 but with notable sediment movements related to its banks and shoals. The seawall was  
53 constructed after the devastating hurricane that occurred in 1900, and extends approximately  
54 16 km from the South Jetty to the southwest direction, and its height is 5 to 6m (Doran et al.,  
55 2009), providing protection from storm surge and wave action mainly to the city of  
56 Galveston. In the middle of the 20<sup>th</sup> century 15 groynes were constructed to maintain the  
57 sandy beach, both for recreational purposes and as scour protection for the seawall. The  
58 direction of net longshore sediment transport along most of the northern and central Texas  
59 coastline is to the southwest (Hall, 1976; Mason, 1981) but a divergent nodal zone (reversal  
60 in net direction) is present in the vicinity of the western portion of Galveston seawall. East of  
61 this region net sediment transport is in a northeasterly direction toward South Jetty and the  
62 entrance of the Bolivar Roads ship channel (King, 2007; Morang, 2006), whereas west of the  
63 nodal zone net transport is directed toward the west end of Galveston Island and San Luis  
64 Pass (Frey et al., 2014), as indicated in Fig. 1.

65

66 Fig. 1.

67

## 68 **1.2. Post-storm beach recovery**

69 Following beach erosion that may be caused in Galveston island by storm events, the natural  
70 process of beach recovery takes place. Generally, beach recovery is a composite phenomenon  
71 affecting the whole beach profile from the lower shoreface and nearshore to the coastline, the  
72 backshore, and dunes. Different natural mechanisms dominate beach recovery in different  
73 parts of a beach, for instance, wave shoaling may cause sediment deposits which had  
74 previously been placed in the lower shoreface to move back towards the shore (Hallermeier,

75 1980, Nielsen and Lord, 1993), while aeolian processes act as the primary restoring force of  
76 eroded backshore and dunes (e.g. McLean and Shen, 2006; Houser and Mathew, 2011).  
77 Although the storm effects on beach morphodynamics have been studied in detail (e.g.,  
78 Larson and Kraus, 1989; Roelvink et al., 2009) beach recovery processes have not yet been  
79 investigated adequately (Jensen et al., 2009; Corbella and Stretch, 2012). Beach recovery is  
80 characterized by some factors such as the tidal range in a specific site and the corresponding  
81 modal wave energy (Phillips, 2018); the first refers to tidal currents that potentially push back  
82 sediment material towards the shore, that was previously driven offshore-wards due to storm  
83 forcing, while the second one to the available wave energy in a coastal site that may mobilize  
84 sediment materials deposited offshore, towards the upper beach. The aforementioned  
85 characteristics, as well as other site specific quantities such as the grain size of the beach  
86 material, determine the duration of beach recovery which can vary from few months to  
87 several years (e.g. Kobayashi and Jung, 2012; Philips et al., 2015). Recovery can be longer  
88 still; for instance Flemming and Davis (1994) reported that the shoreline at Spiekeroog Island  
89 near northern Holland exhibits beach recovery after storm erosion over a period of 11 to 14  
90 years.

91 Galveston beach is characterized by low wave energy (Short and Woodroffe, 2009) and is a  
92 microtidal one (Davies, 1980) as it is located in the Gulf of Mexico. Following a storm event,  
93 the observed recovery duration of the Galveston shoreline and berm varies from few months  
94 to one year (Morton et al., 1994), while the corresponding recovery duration of the backshore  
95 and dune is about four to five years (Morton and Paine, 1985; Morton et al., 1994). However,  
96 Hurricane Ike which made a landfall in Galveston Island in 2008 caused a prolonged  
97 shoreline recovery process which took many years to be completed as will be shown in the  
98 following sections of this study. Therefore, Galveston beach was investigated aiming at

99 understanding the underlying physical mechanisms of its morphodynamic evolution  
100 following Hurricane Ike in 2008.

101

## 102 **2. The study area**

103 Nearshore geological surveys around Galveston Island have indicated that longshore  
104 transport rates of 115,000 m<sup>3</sup>/yr are typical, (having been of this order for several millennia),  
105 and that washover rates are negligible, (Wallace et al. 2010). The Galveston coastal region is  
106 quite limited in terms of sediment supply from rivers. Specifically, most sandy material  
107 carried by the Trinity River is deposited in Lake Livingston (Phillips and Musselman, 2003)  
108 and sediment from the lower Trinity River is accommodated within the delta in Trinity Bay  
109 (Phillips et al., 2004) and does not reach the Gulf of Mexico shoreline. The Brazos River to  
110 the southwest of Follet's Island, the island adjacent to Galveston, carries a much reduced  
111 sediment load due to damming (Dunne and Raines, 2001), and in addition, its mouth has been  
112 relocated further west in an effort to reduce maintenance on the Freeport harbour entrance  
113 (Kraus and Lin, 2002). Fig. 2 summarizes the geographical configuration of the main  
114 locations and key features.

115

116 Fig. 2.

117

118 Evidence presented by King (2007) suggests that sand present in the Bolivar Roads ship  
119 channel, along the Gulf of Mexico beaches and in the surf zone of Galveston Island is either  
120 reworked from relic deposits or remains within the shoreline as it retreated landward at the  
121 end of the last ice age. This leaves the coastal zone in the area sand-limited, consisting only  
122 of a thin sand veneer perched on a mud substrate, with minimal new supply entering the  
123 system (Frey et al., 2014). The latter might come from Galveston Entrance Channel which is

124 regularly dredged by the USACE with the intention of maintaining the navigation channel,  
125 with the dredged material deposited in the vicinity of the seaward tip of South Jetty.  
126 Sediment transport along the Gulf coast shoreline is driven by wave-induced nearshore  
127 currents and depends heavily on the complex offshore bathymetry which modifies  
128 approaching wave fields through refraction and diffraction. Therefore, it is not surprising that  
129 an erosional trend has been observed over time along most of the Galveston beaches while  
130 accretion has occurred on both ends of Galveston. Specifically, the unprotected shoreline  
131 between the western tip of the seawall and San Luis Pass (Fig. 1) was found to be retreating  
132 at moderate rates between  $0.6$  to  $2.0$   $m/yr$  with some portions of Galveston's west end near  
133 the western end of the seawall retreating at rates higher than  $2.0$   $m/yr$ , while stretches  
134 protected by the seawall were considered stable, in part due to occasional nourishment  
135 efforts, (Paine et al., 2011; Gibeaut, 2011). Both ends of Galveston Island and the western  
136 end of the Bolivar Peninsula have been observed to accrete at rates of up to  $5$   $m/yr$  (Paine,  
137 2011).

138 The sediment in the nearshore zone is made up of sand (84 %) and fines (16 %). The coastal  
139 sand residing in the system is very fine with a median diameter  $D_{50}$  around  $0.15$   $mm$  (Frey et  
140 al., 2014). Offshore sediments outside the active surf zone along the coastline are largely  
141 mud-dominated but some limited pockets of beach quality sand exist (White et al., 1985;  
142 Siringan and Anderson, 1994; Anderson and Wellner, 2002; Finkl et al., 2004; Williams et  
143 al., 2012). Offshore beach quality sand is contained mainly in features like Heald Bank (55  
144 km offshore) or Sabine Bank (110 km offshore) with an estimated 585 million cubic metres  
145 and 1.2 billion cubic metres of material, respectively (Morton et al., 1994).

146 Hurricane Ike made landfall at the eastern part of Galveston Island (Hawkes and Horton,  
147 2012) over the western part of Bolivar Peninsula (Sherman et al., 2013), as an extreme  
148 Category 2 hurricane on the 13<sup>th</sup> of September 2008. Hurricane Ike passed through Galveston

149 Bay leaving Houston to its left side while propagating further onto the mainland (Hawkes and  
150 Horton 2012). The path of Hurricane Ike was tracked by Rego and Li (2010) and Sherman et  
151 al. (2013), and shown in Figure 3.

152

153 Fig. 3.

154

155 Extreme events such as hurricanes can have a significant effect on sediment budgets by  
156 transporting large volumes of sediment onshore into the bay (barrier island rollover) or  
157 offshore via shore face erosion or surge ebb flow (e.g., Sallenger, 2000; Morton et al., 2003;  
158 Houser et al., 2008). Goff et al. (2010) showed that storm surge ebb flows across the Bolivar  
159 Peninsula, near Galveston Island, moved sediment far enough offshore during Hurricane Ike  
160 that they were lost to the beach and barrier system.

161 The unprotected part of Galveston Island, west of the seawall, is comprised of sandy beaches  
162 with dunes rising about 2 to 4 m above sea level. This area suffered the erosive impacts of  
163 Hurricane Ike to a greater degree than the region protected by the seawall and the groyne  
164 field, although the sandy beach in front of the seawall also experienced significant erosion,  
165 (Doran et al., 2009). Fig. 4 illustrates erosion caused by Hurricane Ike in front of the seawall  
166 and the groyne field (Fig. 4a and 4b), and near South Jetty (Fig. 4c and 4d).

167

168 Fig. 4.

169

170 In the aftermath of Hurricane Ike bathymetric surveys were commissioned by the Galveston  
171 Park Board of Trustees over the period 2010-2016. For the purposes of this study, the  
172 corresponding shorelines were derived from this data. The details of the data processing are  
173 presented in Appendix A. In addition, a shoreline corresponding to May 2008 (slightly before

174 the occurrence of Hurricane Ike) was identified on Google Earth and consequently was  
175 plotted in the same coordinate system that was used for the post-hurricane historical  
176 shorelines. The shoreline in May 2008 acted as a reference for assessing the degree that  
177 Galveston beach recovered following Hurricane Ike. Fig. 5a shows the sequence of shorelines  
178 between 2008-2016, while Fig. 5b shows the changes relative to May 2008, (by subtracting  
179 the ordinates  $y_{i,2008}$  of the 2008 shoreline from the corresponding ordinates of the shorelines  
180 in the years between 2010-2016, where  $i=1,2,\dots$  is the enumeration of grid points on the X'  
181 axis). Where changes are negative the beach is still revering from its 2008 position, while  
182 where changes are positive the beach has more than recovered.

183

184 Fig. 5.

185

186 Fig. 5a illustrates a conspicuous accumulation of sediment material along the entire beach,  
187 from 2010 to 2014. Fig. 5b shows that apart from the beach sections on the right hand-side  
188 and near South Jetty and Groyne 1, respectively, there is incomplete beach recovery. The area  
189 between the accretive zone near South Jetty and Groyne 14 exhibits slower recovery than the  
190 rest of the groyne field. This trend is verified from Google Earth images. For example, Fig. 6  
191 shows the shoreline evolution in the second groyne compartment counting from South Jetty,  
192 which lies between Groyne 15 and Groyne 14 in Fig. 5, confirming the trend.

193

194 Fig. 6.

195

### 196 **3. Methodology**

197 A one-line modelling framework was adopted as the beach is shaped strongly by longshore  
198 transport, but with alterations made to account for cross-shore removal and addition of



199 sediment. The One-Line model used here is a shoreline model which is based on the  
200 conservation of mass and a longshore sediment transport equation.

201 The one-line model was first proposed by Pelnard-Considère (1956) in his study of beach  
202 behaviour near groynes. In a more formal mathematical treatment Larson et al. (1987)  
203 showed that the equation governing the movement of a single height contour could be  
204 simplified to a diffusion type process under the assumptions of: constant wave direction;  
205 wave crests making small angles with respect to the shoreline trend; small shoreline  
206 gradients; and an initially straight shoreline running parallel to the x-axis. The equation may  
207 be written as:

$$208 \quad \frac{\partial y}{\partial t} = \varepsilon \frac{\partial^2 y}{\partial x^2} \quad (1)$$

209 where  $t$  is time,  $x$  is the longshore distance on an  $X$  axis,  $y$  is the shoreline position on a  $Y'$   
210 axis perpendicular to the  $X'$  axis and  $\varepsilon$  is a diffusion coefficient given by the equation  
211  $\varepsilon=2Q_0/D$ . the quantity  $Q_0$  is the amplitude of longshore sediment transport, and  $D=D_C+D_B$ ,  
212 where  $D_C$  is the depth of closure and  $D_B$  is the berm height. The following extended version  
213 of Eq. (1), (e.g. Hanson, 1987), incorporates a source or sink of sediment material:

$$214 \quad \frac{\partial y}{\partial t} = \varepsilon \frac{\partial^2 y}{\partial x^2} + q_s \quad (2)$$

215 where  $q_s(x,y,t)$  is the sediment transport rate per unit area, coming from a source or a sink  
216 ( $m^3/m/sec$ ).

217 Analytical solutions of Eq. (1) may be found via integral transform techniques for specific  
218 boundary conditions (e.g. Larson et al., 1997). Due to the fairly restrictive assumptions made  
219 in deriving Eq. (1) the applicability of analytical solutions is limited to idealized cases. Over  
220 time, some of these restrictions have been loosened while retaining the benefits of analytical  
221 solutions such as accuracy and the absence of numerical instability, (see e.g. Walton and  
222 Dean, 2011; Valsamidis and Reeve, 2017). Computational solutions to the One-Line model  
223 allow many of the assumptions used in analytical solutions to be lifted. However, they require

224 time-stepping and may exhibit numerical instability, (e.g. Hanson 1987, 1989). An  
225 intermediate approach that lies between analytical and computational approaches is the semi-  
226 analytical solution proposed by Reeve (2006), which provides general analytical solutions  
227 that can be evaluated through numerical integration. These combine some advantages of both  
228 the analytical and the computational solutions; for instance, they can account for time-  
229 varying wave conditions, arbitrarily shaped initial shoreline, and are free of numerical  
230 instability. Here, we construct a site-specific one-line semi-analytical model to describe the  
231 morphodynamic evolution of Galveston beach. Specifically, the semi-analytical solutions for  
232 shoreline evolution near a groyne (Reeve, 2006) and for a groyne compartment  
233 (Zacharioudaki and Reeve, 2008) were combined in conjunction with suitable internal  
234 boundary conditions (BCs), (Valsamidis and Reeve, 2020), to describe the groyne field in  
235 Galveston beach, as depicted in Figure 7.

236

237 Fig. 7.

238

239 The beach from South Jetty westwards to the end of the seawall was represented by 15  
240 groyne compartments plus an open stretch of beach with a single groyne on its lefthand  
241 (eastern) end. The semi-analytical model thus consisted of 15 sets of solutions for groyne  
242 compartments and one solution for a groyne at the end of an open beach; all linked together  
243 to describe the transmission of sediment between adjacent compartments of the model.

244 The details of the semi-analytical solutions for shoreline evolution in groyne compartments  
245 and near a single groyne are presented in Appendix B for ease of reference. These semi-  
246 analytical solutions incorporate arbitrary time-varying boundary conditions.

247 In order to use the semi-analytical solutions to describe the beach movements along  
248 Galveston Island beach it is necessary to describe the processes of material travelling through

249 permeable groynes and also by-passing the tips of the groynes in a manner that can be  
250 incorporated into the solutions, as illustrated in Figure 8.

251

252 Fig. 8.

253

254 A methodology that permits this is that due to Hanson (1989), who proposed scheme to  
255 describe these processes within the framework of a one-line model. The approach is based on  
256 the notion that longshore transport occurs across the cross-sectional profile from shoreline out  
257 to the depth of closure. Under arbitrary instantaneous wave conditions the seaward extent of  
258 longshore transport may not extend as far offshore as the depth of closure. In this case,  
259 Hanson (1989) suggested that the depth of active longshore transport,  $D_{LT}$ , can be estimated

260 from 
$$D_{LT} = \frac{1.27}{\gamma} (H_{s,b}) \quad (3)$$

261 where  $H_{s,b}$  is the significant wave at breaking position; and  $\gamma$  is the wave breaking index.  $D_{LT}$   
262 varies in time according to the variation of  $H_{sb}$ . Let us denote the depth at the tip of the  
263 groyne by  $D_G$ . Further, approximating the beach by a plane slope the following relationships  
264 follow automatically from simple geometrical considerations:

265  $y_{LT} = D_{LT}/sl$  and

266  $y_G = D_G/sl$

267 where  $sl$  is the beach slope in the cross-shore direction,  $y_{LT}$  and  $y_G$  are the distance from the  
268 shore of the depth of active longshore transport and the groyne tip respectively. If  $y_{LT} < y_G$   
269 then no by-passing occurs as the groyne blocks the whole of the section of the profile in  
270 which there is longshore transport. Beach material may still permeate through the trunk of the  
271 groyne, and the amount is determined by the transport rate and the permeability. If  $y_{LT} > y_G$   
272 then by-passing can occur in the region of the cross-section profile for which  $y_G < y < y_{LT}$ . To  
273 estimate the amount of by-passing it is assumed that the longshore transport is spread

274 uniformly across the section of the beach profile for which longshore transport is active. The  
275 by-passing rate,  $Q_{bp}$  is then simply the potential transport rate scaled by the proportion of the  
276 active profile that extends beyond the tip of the groyne:

$$277 \quad Q_{bp} = Q \cdot (y_{LT} - y_G) / y_{LT}$$

278 where  $Q$  is the sediment transport rate determined from a suitable transport formula. This  
279 condition is illustrated in Fig. 9.

280

281 Fig. 9.

282

283 Now, as the groyne lengths are known, and the beach slope is approximately 1% (as  
284 estimated from the bathymetric surveys), the corresponding values of  $D_G$  may be computed  
285 for every groyne. The sediment transport past each groyne, accounting for permeability and  
286 by-passing, can thus be calculated as the sum of the proportion of the longshore transport that  
287 by-passes the groyne plus the product of the proportion of the longshore transport that is  
288 blocked by the groyne, multiplied by the permeability. In symbols:

$$289 \quad F = p(1 - b) + b \tag{4}$$

290 where  $F$  is the total percentage of sediment flux passing from the one modelled area to the  
291 following one,  $p$  is the permeability (as a percentage) of the groyne, and  $b$  is the percentage  
292 of bypassing. The permeability of the groynes was taken to be equal to 30% following the  
293 estimates of Frey et al. (2015).

294 Hourly wave measurements were obtained, from the free online database owned and  
295 maintained by the National Buoy Center, for Station 42035 which is located 22 NM east of  
296 Galveston Island, where the water depth is 15.8 m. The records consist of significant wave  
297 height, peak period and mean wave direction. Wave transformations were performed along a

298 seabed cross-section from the buoy towards Galveston beach via a simple refraction-shoaling  
299 calculation which is described by Valsamidis et al. (2013), and is presented in Appendix C.  
300 The frequency distribution of waves by direction over the period 2010 to 2015 is shown in  
301 Fig. 10, where angles are measured relative to the shore normal. The predominant wave  
302 direction would be expected to cause littoral drift towards the South Jetty, as is observed in  
303 practice.

304

305 Fig. 10.

306

307 It remains to determine the potential longshore transport rate. Several formulae are available  
308 for this purpose and here we have used the CERC formula (CERC, 1984). The diffusion  
309 coefficient  $\varepsilon$  (see Eq. (1)) according to the CERC formula is given by Eq. (5):

$$310 \quad \varepsilon = \frac{K g H_{sb}^2 C g_b}{8(S_g - 1) \lambda (D_c + D_b)} \quad (5)$$

311 where  $K$  is a nondimensional empirical constant,  $C g_b$  ( $m/sec$ ) is the wave breaking celerity,  
312  $C g_b = \sqrt{g D_b}$ ,  $D_b$  is the wave breaking water depth and a typical value was considered equal  
313 to  $1m$ ,  $S_g$  is the specific gravity and is a dimensionless quantity which is equal to  $2.65$ ,  $g$  is the  
314 acceleration of gravity and is equal to  $9.81 m/sec^2$ ,  $D_c$  is the depth of closure and  $D_b$  is the  
315 berm height with values equal to  $D_c = 6.10m$  ( $20 ft$ ) and  $D_b = 1.22 m$  ( $4 ft$ ), (Frey et al., 2015).

316 The model was calibrated over the period April 2010 to April 2011. The measured wave  
317 sequence from the offshore buoy was transformed to the nearshore to drive the 1-line model.  
318 No additional sources of material were introduced in this process and the calibration  
319 consisted of varying the parameter  $K$  in the range between  $0.005$  and  $0.90$ . The value giving  
320 the best results was  $K = 0.05$ .

321 In the absence of additional information we have adopted a simple approach to represent the  
322 accretional trend observed in the groyne compartments, between South Jetty and Groyne 1.

323 That is, material is assumed to be added uniformly across each groyne compartment at a  
 324 constant rate. Mathematically, this is implemented in Eqs (B1) and (B4) by specifying linear  
 325 source terms  $s(x,t)$  for every groyne compartment, corresponding to the  $q(t)$  calibrating values  
 326 that are discussed in Section 4. Source terms,  $s(x,t)$ , are given in  $m/week$ , by the following Eq.  
 327 (6):

$$328 \quad s = \frac{q_s}{(D_c + D_B)} \quad (6)$$

329 As the accretion in the first groyne compartment (between South Jetty and Groyne 15) is  
 330 strongly weighted towards the South Jetty side the uniform distribution in this compartment  
 331 was modified through an additional term of the form  $-(1-x/L)$ . In Table 1, the finite Fourier  
 332 cosine transformations that were used are summarized:

Original function	Transformed via finite Fourier cosines
$I$	$2$ if $\psi=0$ or $0$ if $\psi=1,2,3\dots$
$-(1-x/L)$	$-\left[\frac{1}{2} + \frac{4}{\pi^2} \cos\left(\frac{\pi\psi}{L}\right) + \frac{1}{9} \cos\left(\frac{3\pi\psi}{L}\right) + \frac{1}{25} \cos\left(\frac{5\pi\psi}{L}\right) + \dots\right]$

333 Table 1: The functions which were used for the description of the  $s(x,t)$  function, and their  
 334 finite Fourier cosine transformations.

335 The total source sediment discharge rate in the first groyne compartment between South Jetty  
 336 and Groyne 15 was distributed in a proportion 80% to 20%. Specifically, the transformed  
 337 source terms became, for  $\psi=0$ :

$$338 \quad \hat{s}(\psi, w) = \alpha * 2 - \beta * \left[ \frac{1}{2} + \frac{4}{\pi^2} \cos\left(\frac{\pi\psi}{L}\right) + \frac{1}{9} \cos\left(\frac{3\pi\psi}{L}\right) + \frac{1}{25} \cos\left(\frac{5\pi\psi}{L}\right) + \dots \right] \quad (7)$$

339 while, for  $\psi=1,2,3\dots$ :

$$340 \quad \hat{s}(\psi, w) = -\beta * \left[ \frac{1}{2} + \frac{4}{\pi^2} \cos\left(\frac{\pi\psi}{L}\right) + \frac{1}{9} \cos\left(\frac{3\pi\psi}{L}\right) + \frac{1}{25} \cos\left(\frac{5\pi\psi}{L}\right) + \dots \right] \quad (8)$$

341 where  $\alpha$  ( $=0.8$ ) corresponds to the weighting of the uniform source term along the groyne  
 342 compartment and  $\beta$  ( $=0.2$ ) corresponds to the weighting of the additional source term close to  
 343 South Jetty.

344 The term appearing in Eq. (B1),  $\hat{s}(0, w) = \int_0^a s(x, w) dx$ , simplifies as follows:

$$\begin{aligned}
345 \quad \hat{s}(0, w) &= \int_0^a a * 1 * s - \beta * s * \left(1 - \frac{x}{L}\right) dx \Rightarrow \hat{s}(0, w) = a * s * L - \beta * s * \left[x - \frac{x^2}{2L}\right]_0^L \\
346 \quad \Rightarrow \hat{s}(0, w) &= \left(a - \frac{\beta}{2}\right) * s * L \tag{9}
\end{aligned}$$

347 Corresponding expressions were used for the uniform sources in the remaining groyne  
348 compartments.

349 Solutions were computed at intervals of 1 week to provide a reasonable temporal resolution.

350 A grid of 764 points was used to represent the longshore domain. The calculations took  
351 approximately 30 minutes to determine solutions over the period April 2010 – April 2011 on  
352 a computer with an Intel(R) Core (TM) i7-7600U CPU 2.8 GHz processor and 16 GB RAM.

353

#### 354 **4. Results**

355 The calibrated model results are shown in Fig. 11, for the case of no sediment source terms. It  
356 is clear that the conspicuous trend of accretion, which is more apparent along the first groyne  
357 compartment between the South Jetty and Groyne 15, but also occurs to a lesser degree in the  
358 other groyne compartments, is not captured by just longshore transport alone.

359

360 Fig. 11.

361

362 The Root Mean Square Error (RMSE) was relatively high in this case and equal to *20.6m*.

363 The discrepancy clearly lies in an underestimation of the total sediment volume on the beach.

364 The underprediction of sediment volume suggests that a source of sediment supply has been  
365 omitted in the modelling process.

366 The surveys showed a generally accretive trend along Galveston beach from 2010 to 2014,  
367 while from 2014 to 2016 the shorefront was fairly stable. The observed accretive trend from

368 2010 to 2014 is attributed to a natural beach recovery process following the landfall of

369 Hurricane Ike in 2008 close to South Jetty, augmented by dumping of dredgings near South

370 Jetty as mentioned in the Introduction. It is likely that sediments eroded by Hurricane Ike  
371 were deposited offshore and have since been gradually moved back to the shore by wave  
372 action. The interaction of South Jetty with tidal currents is likely to set up a gyre in residual  
373 currents off the tip of South Jetty that would act to accumulate sediments. However, the  
374 spatial distribution of the deposits is unknown. By using recent wave observations and the  
375 one-line modelling, we can investigate how different patterns of sediment supply match with  
376 the observed beach recovery, and thereby infer the likely spatial distribution of the nearshore  
377 deposits. These sources are incorporated in the One-Line model in Eq. (2) and correspond to  
378 the term  $q_s$  that describes a source or sink of sediment.

379 Given this, and the eastward net littoral drift it is unlikely that material was fed solely from a  
380 distinct store of material near South Jetty, as this would not spread westwards to nourish the  
381 beaches in the groyne field and beyond. An alternative scenario, Scenario 1, is a distinct store  
382 offshore of the nodal point. This could feed the beaches to the west of the groyne field and,  
383 with sufficient permeability and by-passing, potentially nourish the beaches in the groyne  
384 field, as well as creating an accumulation near South Jetty due to its interruption of the  
385 longshore drift. The difficulty with this scenario is that there is no obvious geomorphological  
386 driver that would provide a mechanism to select the nodal point as the place for preferential  
387 deposition resulting from Hurricane Ike. An alternative, Scenario 2, would have a distinct  
388 store near South Jetty, plus a diffuse store running the length of the remainder of the beach in  
389 the form of an offshore shore-parallel sand bar. This would correspond to the situation in the  
390 first scenario plus a uniform removal of sediment by Hurricane Ike and subsequent gradual  
391 feeding of the shoreline.

392 Scenario 1:

393 In this scenario a single large supply of sediment material is created on the western side of  
394 the groyne field to investigate whether this could produce the observed accretion within the



395 groyne field up to the South Jetty, relying on the predominant littoral drift. A sediment source  
396 was modelled on the western side of the groyne field such that the beach was supplied with  
397 an equal amount of sediment material (integrated over time and length of the source) with the  
398 one which was applied in the groyne compartment between the South Jetty and Groyne 15 in  
399 Scenario 2 (see Fig.14). The simulation was performed over the period 2011-2015  
400 considering no other sources along the beach. The sediment was supplied uniformly along  
401 this beach section at a rate that decreased with time, in a manner identical to that described in  
402 Scenario 2 below. As illustrated by the results in Fig.12, sediment is not transported in  
403 sufficient quantities through the groyne field towards South Jetty to successfully simulate the  
404 observed accretion. Groyne 1 acts effectively to interrupt the longshore transport, resulting in  
405 accretion of the beach west of Groyne 1 and very little accretion of the beach within the  
406 groyne field or near South Jetty.

407

408 Fig. 12.

409

410 We thus conclude that the recovery of the beach is not due to an isolated supply of sediment  
411 to the west of the groyne field and further, it seems that an additional source of sediment is  
412 necessary to account for the observed accretion near South Jetty.

413 Scenario 2:

414 In this scenario a sand bank located near South Jetty and a sand bar offshore of Galveston  
415 beach are assumed to have been formed as illustrated in Figure 13. The sand bank is located  
416 near South Jetty and is hypothesized to have nourished the area between South Jetty and  
417 Groyne 15 up to 2014 (Fig. 5). The sand bar is assumed to be located offshore of the groyne  
418 field, and to feed the coastal area between Groyne 15 and Groyne 1.

419

420 Fig. 13.

421

422 The form, timing and volume of the sediment supply is unknown, leaving a myriad of  
423 possibilities that could be hypothesised. To investigate the impact of different sediment  
424 supply on the beach evolution several sub-scenarios were envisioned. To this end, linear  
425 sources of sediment were specified, causing accretion uniformly within in every groyne  
426 compartment of the groyne field, from the South Jetty to Groyne 1. Furthermore, from Fig. 5  
427 it can be intimated that the accretion rate in the first groyne compartment, between South  
428 Jetty and Groyne 15, is not constant but rather decreases over time; specifically, the observed  
429 accretion rate in 2010-2011 is greater than the corresponding one in 2011-2015, while after  
430 2014 it is almost diminished. To mimic this behaviour, for the first groyne compartment only,  
431 a decreasing rate of sediment flux was considered with an exponential form  $AExp\{-Bt + C\}$ .  
432 The constants  $A$ ,  $B$  and  $C$  were varied systematically to achieve a best fit for the period 2010  
433 to 2011. The form shown in Fig.14 provided the closest recreation of the observed shoreline  
434 change. Also shown are the maximum and minimum sediment fluxes that were used in the  
435 fitting process.

436

437 Fig. 14.

438

439 It is clear from Fig. 14 that while a supply to the first groyne compartment can improve the  
440 prediction of the observed beach position in this area, it has little impact on the beach  
441 position in the remaining compartments, indicating that material added at this part of the  
442 beach does not travel easily further westwards towards the seawall; a conclusion that would  
443 be expected from the prevailing littoral transport direction.

444

445 For all remaining groyne compartments, constant rates of sediment flux were applied to  
446 mimic the gradual accretion observed in these areas (Fig. 5). Specifically, in the second  
447 groyne compartment between Groyne 15 and Groyne 14,  $q_2$  values were tested for the range  
448  $1 \leq q_2 \leq 10 \text{ m}^3/\text{week}$  and the optimum value  $q_2 = 2.52 \text{ m}^3/\text{week}$  found. Regarding the other groyne  
449 compartments up to Groyne 1, the following values of sediment flux rate were chosen:  $q_3 =$   
450  $q_4 = \dots = q_{14} = 1.08 \text{ m}^3/\text{week}$ , considering values in the range:  $0.5 \leq q_i \leq 5 \text{ m}^3/\text{week}$ , where  
451  $i = 3, 4, \dots, 14$ . Results from the semi-analytical model for the best-fit case are presented in  
452 Fig.15.

453

454 Fig. 15.

455

456 The Root Mean Square Error (RMSE) corresponding in this fitting process was  
457  $RMSE = 13.85m$ .

458 The above process does not constitute a formal optimization procedure but provides a  
459 systematic approach to optimize the simulation results with the assumed form of sediment  
460 source distribution. As a check on the assumed source distribution, with the best case  
461 scenario distribution of sources found above, the model was ‘validated’ over the time period  
462 April 2011 – May 2015. The results are shown in Fig. 16 and the corresponding  $RMSE$  was  
463  $16.13m$ .

464

465 Fig. 16.

466

467 The error in this case, over a four year prediction period, is slightly larger than for the  
468 optimization performed over a one year period, but suggests the hypothesized source  
469 distribution is a plausible one.

470

## 471 **5. Discussion**

472 The accretive trend along Galveston beach which is shown in Figures 5a&b and 6, over the  
473 period 2010 to 2014, followed the significant beach loss caused by Hurricane Ike in 2008  
474 (Fig. 4). As mentioned in Section 2 this area has a limited amount of sediment supply so the  
475 arrival of sediment to the extent shown by the historical surveys over the period 2010 to 2016  
476 is quite remarkable. The recovery period of Galveston beach and dune systems after a major  
477 event like a hurricane has been estimated by Morton et al. (1994) to be approximately 5  
478 years. The observed timescale of accretion occurring from 2010 up to 2014 (Figs.5a&b)  
479 along Galveston beach agrees well with this.

480 In addition, as is evident from Fig. 5a&b, there is a larger amount of accretion occurring near  
481 the South Jetty in comparison with the rest of the beach. This may be due to the fact that as  
482 Hurricane Ike passed over Galveston Bay (Doran et al., 2009; Rego and Li, 2010; Hawkes  
483 and Horton, 2012), sediment material moved offshore from Galveston beach, (Sherman et al.,  
484 2013), but also through the inlet of Bolivar Roads and towards the offshore tip of South Jetty,  
485 ( Goff et al., 2010). Subsequently, waves could have transported the sediment material which  
486 had earlier been deposited near the tip of the South Jetty back to the eastern part of Galveston  
487 beach. The rate at which this process takes place in the first groyne compartment between the  
488 South Jetty and Groyne 15, decreases in time (Figs. 5a&b), suggesting that the accretion  
489 phenomenon in the first groyne compartment had started earlier than 2010, possibly, almost  
490 straight after the passage of Hurricane Ike in 2008. A similar morphodynamic mechanism can  
491 be envisaged when the dredgings from the Bolivar Road channel is deposited offshore of  
492 South Jetty, forming a sand bank in that area. Then, due to wave action, material is  
493 redistributed in the vicinity of South Jetty, reducing the volume in the sand bank, as  
494 suggested by Frey et al. (2015).

495 Moreover, accretion occurs in the region extending from Groyne 15 to Groyne 1 (Figs.  
496 5a&b); between 2010 and 2014. Thus, it could be hypothesized that while the first groyne  
497 compartment (extending from South Jetty to Groyne 15) is gradually filled with sand,  
498 sediment material is moved along to the other groyne compartments through littoral transport,  
499 permeability of the groynes and by-passing. However, this is most unlikely because the  
500 prevailing wave conditions in the vicinity of the groyne field (Fig. 10) cause a littoral drift  
501 from the end of the groyne field towards the South Jetty.

502 As an alternative, it was hypothesised the existence of a sand bar offshore of the groyne field.  
503 This sand bar is considered to have been formed due to offshore deposits of material that are  
504 gradually brought onshore after the hurricane.

505 Regarding the significant accretion which is observed on the right-hand side of Groyne 1 in  
506 June 2016 (Figs. 5a&b), this is due to the nourishment efforts that were executed westwards  
507 of the groyne field in 2015. Specifically, in March 2015 a beach nourishment was placed at  
508 Dellapena Park, on the west side of the seawall (Guillen, 2017). Moreover, in November  
509 2015 nourishment works were conducted west of 61<sup>st</sup> Street, (the area west and in the  
510 immediate vicinity of Groyne 1, Guillen (2017)).

511 Some caveats are worth noting in regard to the simple modelling framework adopted here.  
512 Firstly, the nearshore wave transformation was simplified by treating the bathymetric  
513 contours as being approximately parallel to the shore. This cannot fully describe the effects of  
514 the complex bathymetry near Galveston beach on local wave refraction and diffraction  
515 effects. Secondly, the sediment transport and response of the beach morphology is modelled  
516 within the framework of a one line model, with the well-known associated restrictions on  
517 detailed process description. In addition, the semi-analytical beach model does not include  
518 spatial variation of breaking wave angle, and so cannot reproduce the effects of wave  
519 diffraction on sediment movement. Another limitation of the current modelling work is that it

520 treats only a single sediment fraction, in this case sand. The implications of this are that in  
521 parts of the case-study where a significant portion of the beach sediment material is not sand,  
522 e.g. near South Jetty where dredged material from the Trinity delta (Fig. 2), which is  
523 predominantly muddy (Davis, 2017), is placed at the offshore tip of the South Jetty, results  
524 may be less reliable. The discrepancies in shoreline prediction close to South Jetty (Fig. 15  
525 and Fig. 16) may be caused by the simplification of wave conditions or variations in sediment  
526 composition. A detailed analysis of these issues is not the purpose of this paper but may be  
527 investigated further in future research.

528 Fig. 5b shows that beach recovery is not full along the shorefront, although in the part of the  
529 groyne field between Groyne 15 and Groyne 1, it occurs to a greater degree than in the first  
530 groyne compartment, especially on the left hand-side of Groyne 15, and in its vicinity. From  
531 Fig. 5a, the historical shorelines appear to be converging towards to a new configuration  
532 along the groyne field, up to 2016. This new beach shape is far away from the shoreline in  
533 2008, so it seems that either some sediment material was permanently lost beyond the depth  
534 of closure due to Hurricane Ike, or, the recovery is still ongoing at this stage.

535 The semi analytical model is quite general in its applicability and is not restricted to  
536 Galveston Island. Indeed, it could be applied, for instance, to Fire Island in New York where  
537 Hurricane Sandy made a landfall in 2012 and which has been the subject of several  
538 geomorphic and modelling studies, (Goff et al., 2015; Warner et al., 2017; Bennett et al.,  
539 2018), and Pea Island Breach located in the Outer Banks of North Carolina, USA, where  
540 Hurricane Irene and Hurricane Sandy made landfall in 2011 and 2012, respectively (Montoya  
541 et al., 2018).

542

543 **Conclusions**

544 A unique set of shoreline surveys has provided the basis for an exploration of the recovery of  
545 Galveston beach after the passage of Hurricane Ike. These, combined with a semi-analytical  
546 one-line model have been used to gain insights into the meso-scale recovery process. An  
547 explanation of the morphodynamic evolution of a section of Galveston beach near the city of  
548 Galveston, extending from South Jetty up to a point along the Seawall approximately 17 km  
549 westwards, has been proposed as a result.

550 The surveys showed a generally accretive trend along Galveston beach from 2010 to 2014,  
551 while from 2014 to 2016 the shorefront was fairly stable. The observed accretive trend from  
552 2010 to 2014 was attributed to a beach recovery process following the landfall of Hurricane  
553 Ike in 2008 close to South Jetty, which caused extended beach erosion. Given the sediment  
554 limited nature of the site the recovery of the beaches is remarkable and is likely due to  
555 material moved and stored in offshore deposits gradually being reworked to the beaches.

556 There are no bathymetric surveys to confirm or refute the existence of such deposits.

557 However, their existence can be inferred from the observed beach recovery and modelling of  
558 the beach evolution.

559 A semi-analytical beach model based on the one-line framework was used to investigate the  
560 beach recovery process. Using local wave conditions covering the period 2010-2015 we have  
561 established that:

- 562 1) It is most unlikely that the beach recovery arose solely through a source of sediment  
563 to the beach west of the groyne field, even though the predominant littoral drift at this  
564 location is predominantly towards the east. The groyne field, although permeable does  
565 not allow sufficient quantities of sand to be transported along the beach to match the  
566 speed of beach recovery;

567 2) A single source of material to the beach near South Jetty does not nourish the groyne  
568 compartments or the beach to the west of the groyne field due to the prevailing littoral  
569 drift to the east;

570 3) The combination of a single source in the compartment nearest South Jetty, with a  
571 spatial weighting towards the jetty, and a distributed set of smaller sources along the  
572 length of the beach provides a better fit to the observations.

573

574 Further, we conclude that:

575 1) Notwithstanding its rather simple description of sediment transport dynamics the One-  
576 Line model provides a useful tool for analysing the medium scale evolution and  
577 response of beaches;

578 2) The version of the one-line model used here is based on analytical solutions for basic  
579 building blocks of solutions for single groynes and groyne compartments, linked  
580 together using time-varying boundary conditions that can account for the permeability  
581 of the groynes and by-passing of the tips of the groynes. This modelling approach has  
582 been shown to be feasible for an extended length of coast with multiple barriers to  
583 littoral drift and arbitrary sources of sediment;

584

## 585 **Acknowledgements**

586 AV and DER acknowledge the support of the UK Engineering and Physical Sciences  
587 Research Council (EPSRC) through the MORPHINE project (grant EP/N007379/1).

588

## 589 **Data access**

590 The shorelines in 2010 and 2011 were created using data sets from the University of Texas  
591 Austin's Bureau of Economic Geology in the Jackson School of Geosciences. Moreover, the



592 Galveston Park Board provided bathymetric data with respect to years 2014, 2015 and 2016.

593 All bathymetric data used in this study is available from Dr Jens Figlus [figlusj@tamu.edu].

594

## 595 **Modelling**

596 The new semi-analytical model has been written as a MATLAB code called AMMOS. The

597 code is available from Dr Valsamidis/Prof Reeve on request.

598 [antonios.valsamidis@swansea.ac.uk / d.e.reeve@swansea.ac.uk].

599

## 600 **Appendix A. Bathymetric data processing to extract historical shorelines**

601 The 2010 & 2011 shoreline data were provided in a GIS database (drawing shp & dbf file)

602 and a coordinate transformation was made (UTM zone 15 to LM projection) in order to be

603 compatible with the rest of the shoreline data (2014-2016).

604 The 2014, 2015 & 2016 shoreline data, were provided in an Autodesk Civil 3D drawing file,

605 derived from the DTMs produced from the original field data measurements, and converted

606 from feet to metres.

607 All shoreline data (coordinates) refer to the NAD83 Texas State Planes, South Central

608 Zone(TX83-SC) coordinate system, using an LM projection and the NAD 83 Datum

609 (horizontal) and to the north America vertical datum of 1988 (NAVD88), and they were

610 plotted in a single drawing (dwg) file.

611 An A-B axis was drawn, (the total length is 16875 metres), along the average shoreline

612 direction, as a reference.

613 The A-B (east to west direction) axis has an original azimuth of *257.6087 grads* and was

614 rotated clockwise along with the shoreline polyline data.

615 The A basepoint coordinates were  $X=1015098.0079$  and  $Y=4173543.9111$  metres and the

616 clockwise rotation angle was *42.3913 grads*, in order to coincide with the *X* axis.

617 The resulting constant  $Y$  value of the rotated  $X$  axis was *4173543.9111* metres.  
618 The shoreline deviation from the rotated A-B axis is the shoreline position relative to the A-B  
619 axis. That is, the ‘y’ value shown in Cartesian plots of the beach.  
620 For ease of reference, the rotated data were transposed to the origin of the Cartesian system  
621 and the shoreline data ( $Y$ -Axis) were re-sampled at fixed intervals along the  $X$ -Axis of *12.5m*.  
622 This resolution was sufficient to capture the main morphological features of the beach while  
623 avoiding undue computing demands for the semi-analytical modelling.

624

## 625 **Appendix B. Semi-analytical solutions - summary**

626 The shoreline evolution in a groyne compartment (Zacharioudaki and Reeve, 2008) is  
627 described by a solution to Eq. (2), which is derived via finite Fourier cosine transforms. This  
628 solution consists of the sum of the following 4 terms:

$$629 \quad y_1^{GC} = \frac{1}{a} \bar{g}(0) + \frac{1}{a} \int_0^t \varepsilon(w) (j(w) - k(w) + \hat{s}(0, w)) dw \quad (\text{B1})$$

$$630 \quad y_2^{GC} = \frac{2}{a} \sum_{\psi=1}^{+\infty} \cos\left(\frac{\psi\pi x}{a}\right) \hat{g}(\psi) \exp\left(-\int_0^t \frac{\pi^2 \psi^2}{a^2} \varepsilon(u) du\right) \quad (\text{B2})$$

$$631 \quad y_3^{GC} = \frac{2}{a} \sum_{\psi=1}^{+\infty} \cos\left(\frac{\psi\pi x}{a}\right) \int_0^t \exp\left(-\int_w^t \varepsilon(u) \left(\frac{\psi\pi}{a}\right)^2 du\right) (\varepsilon(u) \left((-1)^\psi j(w) - k(w)\right)) dw \quad (\text{B3})$$

$$632 \quad y_4^{GC} = \frac{2}{a} \sum_{\psi=1}^{+\infty} \cos\left(\frac{\psi\pi x}{a}\right) \int_0^t \exp\left(-\int_w^t \varepsilon(u) \left(\frac{\psi\pi}{a}\right)^2 du\right) \hat{s}(\psi, w) dw \quad (\text{B4})$$

633 In the above equations  $g(x)$  corresponds to the initial shoreline position,  $\hat{g}(\psi) =$

634  $\int_0^a g(x) \cos\left(\frac{\psi\pi x}{a}\right) dx$  thus,  $\hat{g}(0) = \int_0^a g(x) dx$ ; ‘a’ refers to the groyne compartment’s

635 length;  $\hat{g}(\psi)$  is the finite-Fourier cosine transform of  $g(x)$ ;  $\psi$  is an integer transform variable;

636  $j(w)$  is the time-varying boundary condition on the left side of the groyne compartment;  $k(w)$

637 is the corresponding boundary condition on the right side of the groyne compartment;  $w$  is a

638 dummy variable of integration running from time  $0$  to arbitrary time  $t$ . The integrals with

639 respect to  $u$  yield a number for a given value of  $t$  while those with respect to  $w$  require

640 numerical evaluation. Finally, the source term appearing in Eq. (6) is given by:  $\hat{s}(0, w) =$

641  $\int_0^a s(x, w) dx$

642 The term  $y_2^{GC}$  incorporates the initial shoreline shape while  $y_3^{GC}$  the boundary conditions at

643 the groynes. The source term is described by the fourth term  $y_4^{GC}$ . However, the term  $y_1^{GC}$

644 involves the initial shoreline position, the source term and the boundary conditions.

645 Finally, the shoreline evolution in a groyne compartment is given by the summation of Eqs.

646 (B1)-(B4):

647  $y^{GC} = y_1^{GC} + y_2^{GC} + y_3^{GC} + y_4^{GC}$  (B5)

648 where  $j(w)$  and  $k(w)$  are the boundary conditions on the left-hand side and right-hand side

649 groynes of the groyne compartment, respectively.

650 Similarly, the shoreline evolution near a groyne may be computed via the following equations

651 (Reeve, 2006):

652 This solution consists of the following 3 terms:

653  $y_1^G = \frac{1}{\pi} (\pi \int_0^t \varepsilon(u) du)^{-1/2} \int_0^{+\infty} g(\xi) [\exp\left(-\frac{(x-\xi)^2}{4 \int_0^t \varepsilon(u) du}\right) + \exp\left(-\frac{(x+\xi)^2}{4 \int_0^t \varepsilon(u) du}\right)] d\xi$  (B6)

654 where  $g(x)$  is the initial shoreline position, and  $\xi$  is a dummy variable used in the integration

655 process. In many cases the initial beach is taken as a straight line with  $g(x)=0$  in which case

656 this term is identically zero.  $y_1^G$  describes the contribution of the initial shoreline shape to the

657 consequent evolution;

658  $y_2^G = \frac{2}{\pi} \int_0^{+\infty} (\int_0^t \exp(-\int_w^t [\omega^2 \varepsilon(u)] du) \tilde{q}(\omega, w) dw) \cos(\omega x) d\omega$  (B7)

659 where  $\omega$  is the transform variable used in the Fourier cosine transform operation,  $\tilde{q}$  is the

660 Fourier cosine transformed variable of  $q$ ; the latter parameter describes the sediment flow

661 from a source or sink of sediment discharge, and  $w$  is a variable related to time. This term

662 corresponds to the impact of a source or sink of sediment discharge on shoreline evolution.

663 Again, in case that there are no sources or sinks  $q(t)$  may be considered equal to zero, and the  
 664 second term is zero as well.

$$665 \quad y_3^G = \frac{1}{\sqrt{\pi}} \int_0^t \varepsilon(w) j(w) \left( \frac{1}{\sqrt{\pi \int_w^t \varepsilon(u) du}} \exp\left(-\frac{x^2}{4 \int_w^t \varepsilon(u) du}\right) \right) dw \quad (\text{B8})$$

666 where  $j(w)$  is the boundary condition at the groyne. The third term  $y_3^G$  corresponds to the  
 667 impact of the combination of wave action and the boundary condition at the groyne on the  
 668 shoreline evolution.

669 Finally, the shoreline position is given as the summation of Eqs. (B6), (B7) and (B8):

$$670 \quad y^G = y_1^G + y_2^G + y_3^G \quad (\text{B9})$$

671

## 672 **Appendix C. The wave transformation process**

673 The procedure for every pair of consecutive spatial steps of the selected cross-shore profile,  
 674 starting from its offshore limit, is the following:

675 1. Calculate the refraction coefficient at the seamost point, (depth  $d_1$ ), as:

$$676 \quad K_1 = KH_1 / d_1 \quad (\text{C1})$$

677 Here, Hunt's (1959) approximation was used so:

$$678 \quad KH_1 \approx \sqrt{Y^2 + \frac{Y}{f(Y)}};$$

$$679 \quad f(Y) = (1 + 0.666666Y + 0.355555Y^2 + 0.160846Y^3 + 0.063210Y^4 + 0.021754Y^5 +$$

$$680 \quad 0.006541Y^6);$$

$$681 \quad Y = \frac{v^2 \times d_1}{g};$$

$$682 \quad v = \frac{2\pi}{T};$$

683 and  $T$  is the wave period.

684 2. Similarly, for the adjacent shoreward point, the refraction coefficient is calculated:

$$685 \quad K_2 = KH_2 / d_2 \quad \text{where } d_2 \text{ the water depth at the shoreward point.}$$

686 3. The wave angle at the shoreward point is calculated:

$$687 \quad \varphi_2 = \sin^{-1}(\theta_1) \quad (C2)$$

688 where:  $\theta_1 = K_1/K_2 \times \sin(\varphi_1)$ ;  $\varphi_1$ : wave angle at the offshore point.

689 4. The wave height at the shoreward point,  $H_2$ , is calculated as:

$$690 \quad H_2 = H_1 \times \sqrt{\lambda_{r,s}} \quad (C3)$$

691 where  $\lambda_{r,s}$ , is the combined refraction and shoaling coefficient given by the following  
692 equation:

$$693 \quad 5. \quad \lambda_{r,s} = \frac{(K_2 \times \cos(\varphi_1) \times (1 + 2 \times \frac{KH_1}{\sinh(2 \times KH_1)}))}{(K_1 \times \cos(\varphi_2) \times (1 + 2 \times \frac{KH_2}{\sinh(2 \times KH_2)}))} \quad (C4)$$

694 6. Check for breaking. The wave breaking condition which was to set the breaking index  
695  $\gamma_{0.78} = H_b/d = 0.78$ . In other words, wave heights which were exceeding 78% of the water depth  
696  $d$ , were considered to break, and their height was reduced to  $0.78 \times d$ .

697

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# Figure Captions

Fig. 1. Location map of Galveston Island (Source: Google Earth), lying between the South Jetty of Bolivar Roads and San Luis Pass. The city of Galveston on the northeast side of the island is protected by a seawall (denoted by a double orange line) and a groyne field symbolized by short yellow lines along the beach front. Orange arrows denote the direction of 2 different littoral drifts; one heads SW towards the San Luis Pass, and one in the opposite NE direction towards the South Jetty. However, a nodal zone near the western side of Seawall, indicated by a yellow ellipse, is the region of drift divergence.



Fig. 2. Coastal setting of Galveston Island: (a) Location of Galveston Island in the Gulf of Mexico; (b) Brazos River discharges near Free Harbour Entrance, while Upper Trinity River and Lower Trinity River discharge into Lake Livingstone and Trinity Bay, respectively; (c) The area in the vicinity of Galveston Island. (Source: Google Earth)

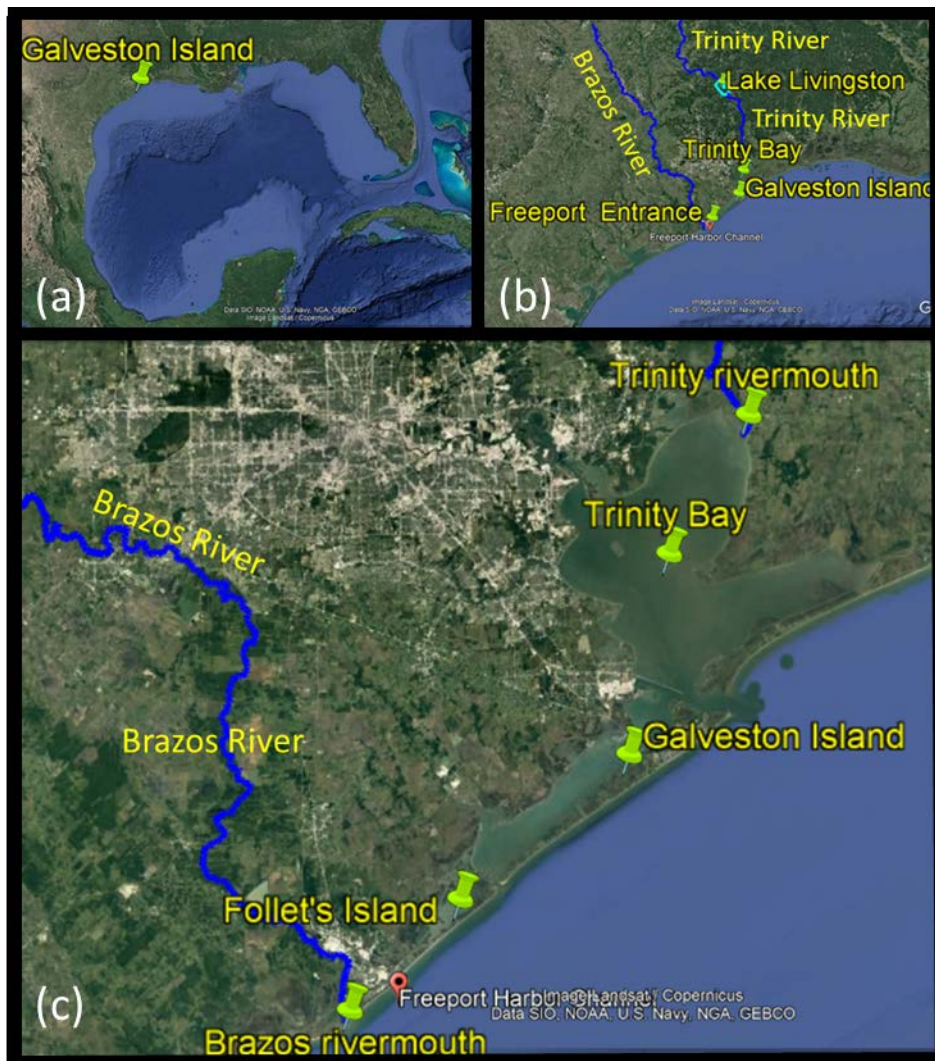


Fig. 3. Hurricane Ike's track as depicted: (a) by Rego and Li (2010), passing over the eastern part of Galveston Island; and (b) by Sherman et al. (2013) considering Hurricane Ike making landfall over Bolivar Peninsula and close to the eastern side of Galveston Island.

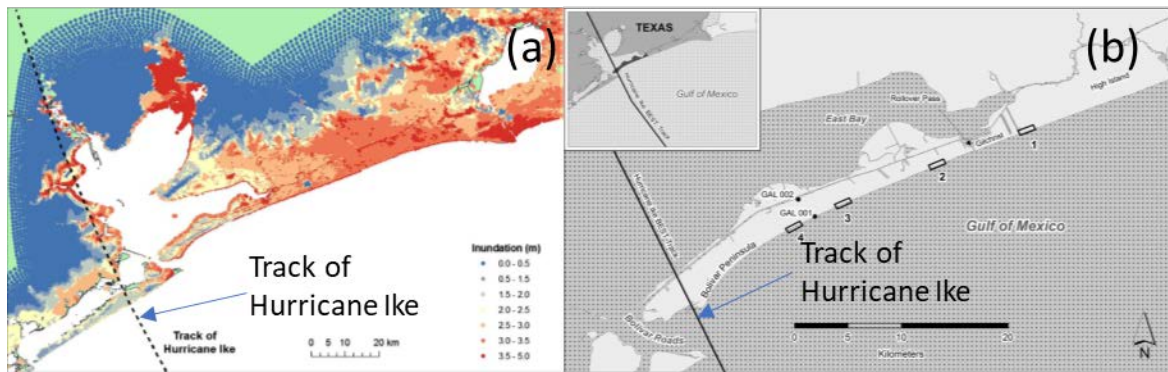




Fig. 4. (from Doran et al., 2009): Photos of the sandy beach and the pier in front of the Galveston seawall on September 10, 2008 (a) and 5 days later (September 15, 2008). The pier structure was destroyed and large volumes of sand from the upper beach section had been eroded during the passage of Hurricane Ike on the 13<sup>th</sup> of September 2008 (b). Yellow arrows denote reference points used for comparison purposes. Similarly, photos of Galveston beach near the South Jetty on the 10<sup>th</sup> of September (c) and the 15<sup>th</sup> of September (d) are compared; here the effects of Hurricane Ike on the beach are more conspicuous.



Fig. 5. (a) Surveyed historical shoreline positions on Galveston Island. The black vertical lines show groyne locations. 15 groynes in total have been constructed and they are enumerated from 1 (terminal groyne) up to 15 (the nearest groyne to South Jetty). (b) Relevant shoreline positions for the years 2010, 2011, 2014, 2015 and 2016 have been plotted with respect to the August 2008 shoreline. Negative values show incomplete beach recovery following Hurricane Ike while positive values denote shoreline advance beyond the

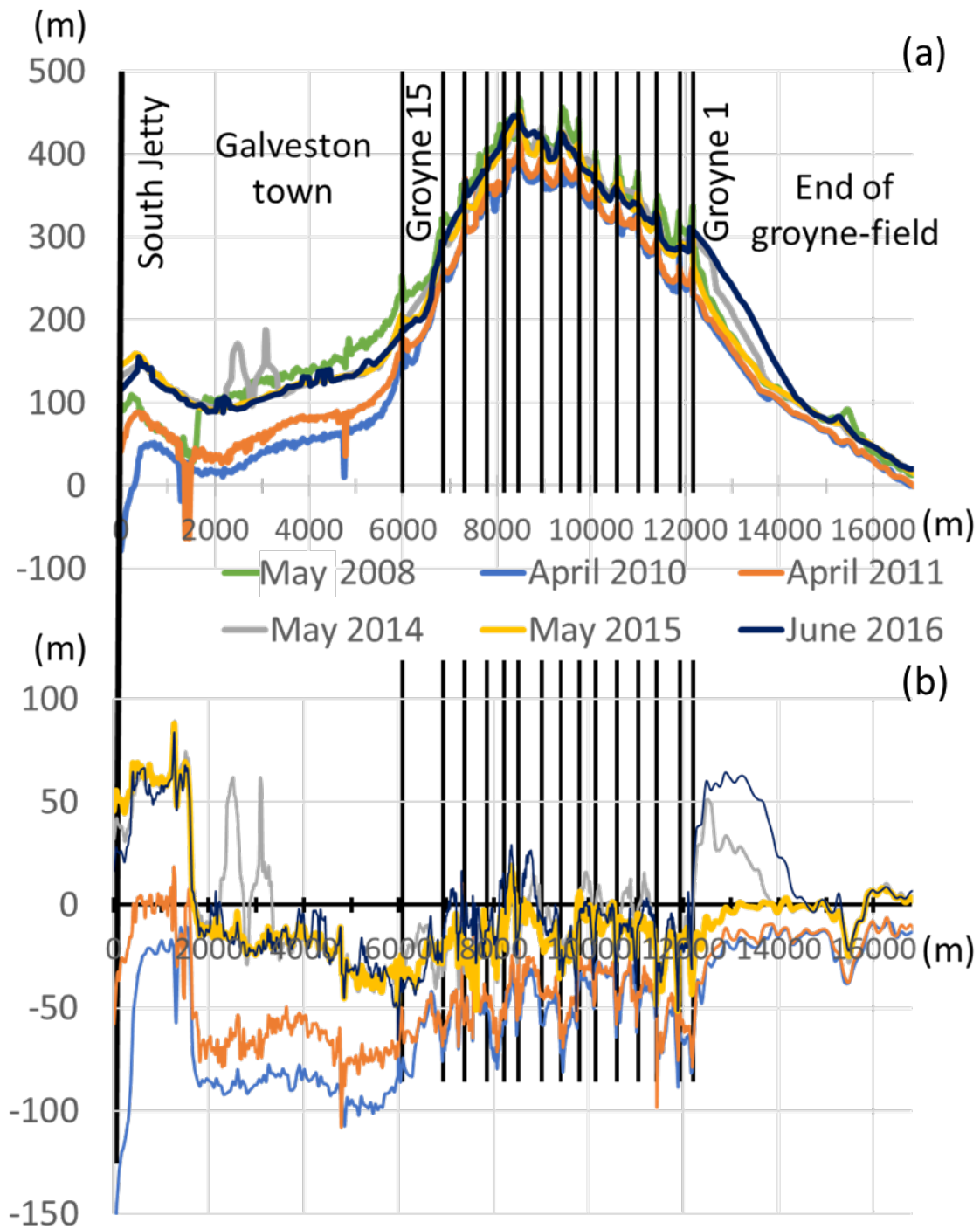




Fig. 6. Shoreline evolution in the 2nd groyne-compartment: the blue line corresponds to April 2010; the orange line to April 2011; the gray line to May 2014; the yellow line to May 2015; and the purple line to June 2016.



Fig. 7. Schematic illustration of the construction of the beach model for Galveston Island from solutions for groyne compartments and single groynes. The elements are connected using suitable boundary conditions (described in the main text below). The black lines illustrate possible shoreline positions in each area of the domain.

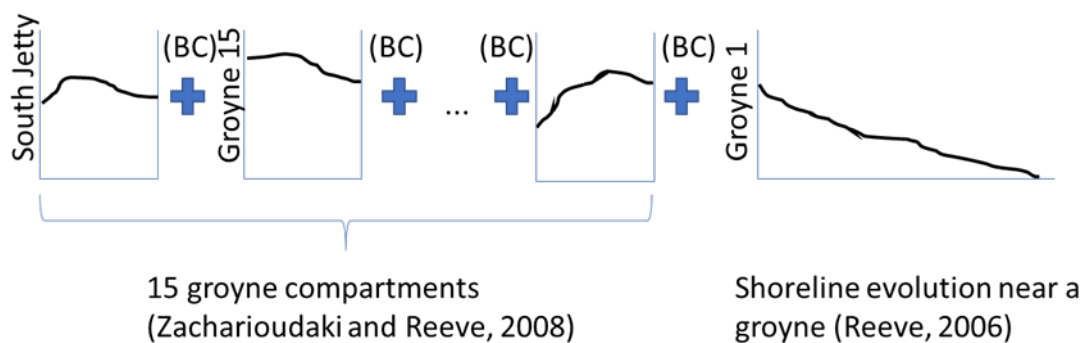


Fig. 8. Simultaneous sediment bypassing of the seaward tip of a groyne and sediment passing through the trunk of a permeable groyne.

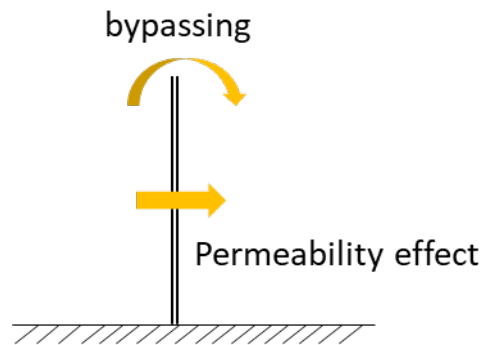


Fig. 9. A wave event  $W$  causing longshore sediment movement (denoted with the orange arrows) up to the depth of active longshore sediment transport  $D_{LT}$ . As  $D_{LT} > D_G$ , or equivalently  $y_{LT} > y_G$ , sediment bypassing occurs.

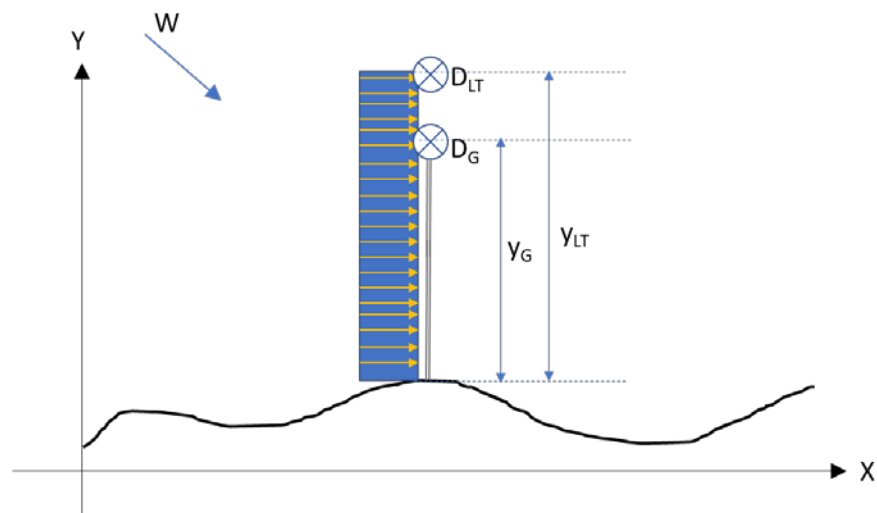


Fig. 10. A rose diagram showing the wave direction distribution over the period 2010 – 2015 for Galveston Island.

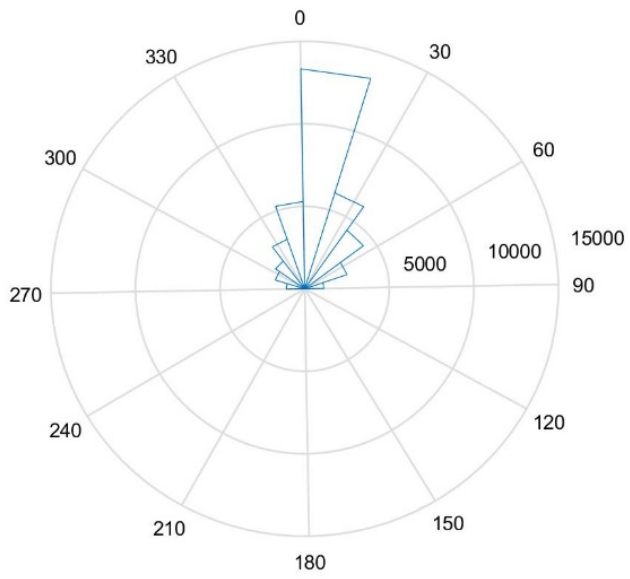


Fig. 11. Calibrated model simulation of Galveston beach over the time period 2010 – 2011. (a) The initial condition is shown in blue, the measured shoreline in April 2011 in orange and the simulated shoreline for April 2011 in grey. (b) The corresponding relative shorelines, considering the reference shoreline in August 2008.

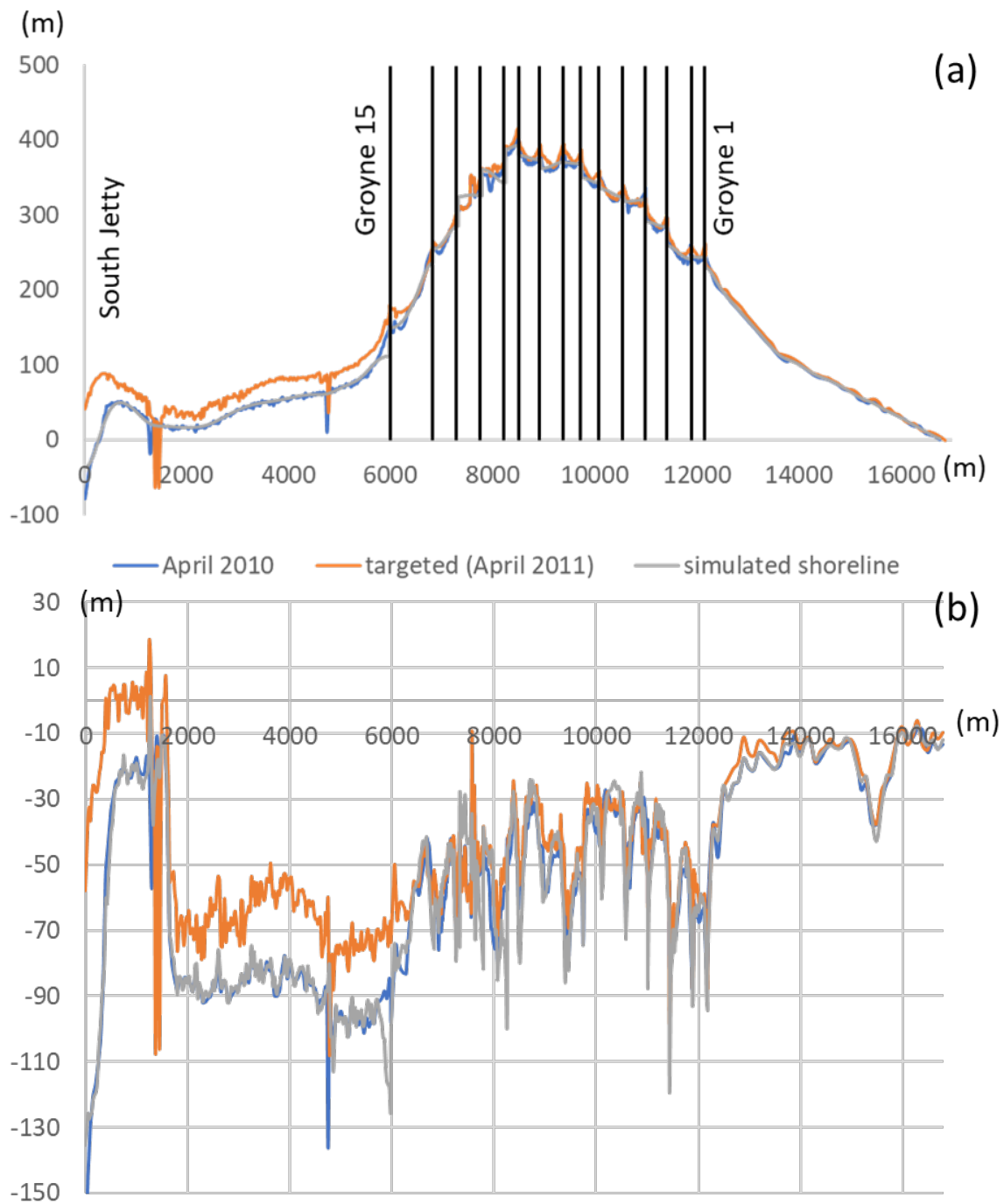


Fig. 12. Results of the simulation of Scenario 1 over the period 2011 to 2015. (a) The blue line represents the initial shoreline position in April 2011, the orange one the targeted shoreline position in April 2015 and the grey line the simulated shoreline in April 2015. (b) The corresponding relative shorelines, considering the reference shoreline in August 2008.

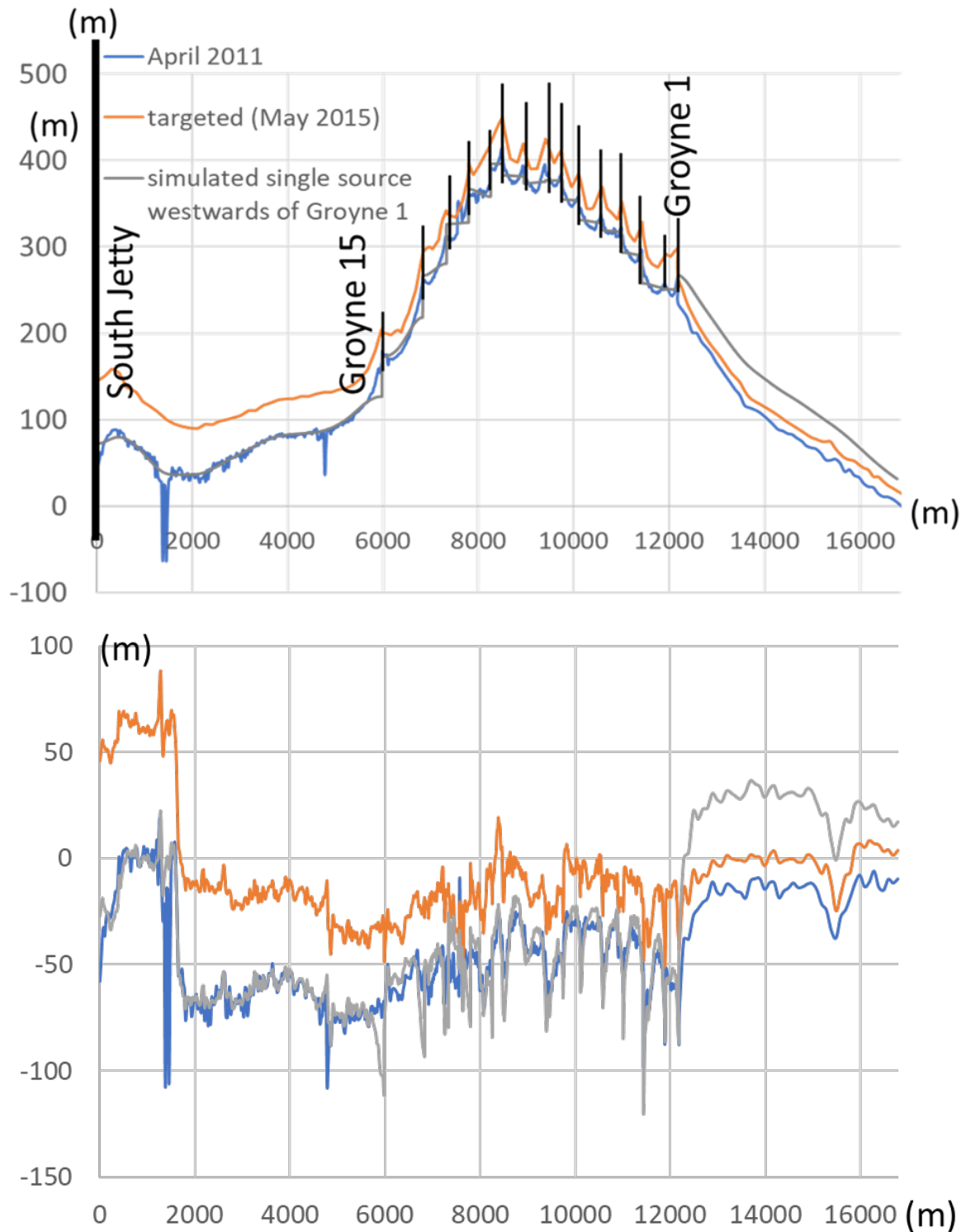


Fig. 13. Distribution of sand sources in Scenario 2 where a sand bank nourishes the area between South Jetty and Groyne 15 and a sand bar nourishes the beach along the groyne field. The yellow thick bars denote the locations of groynes.

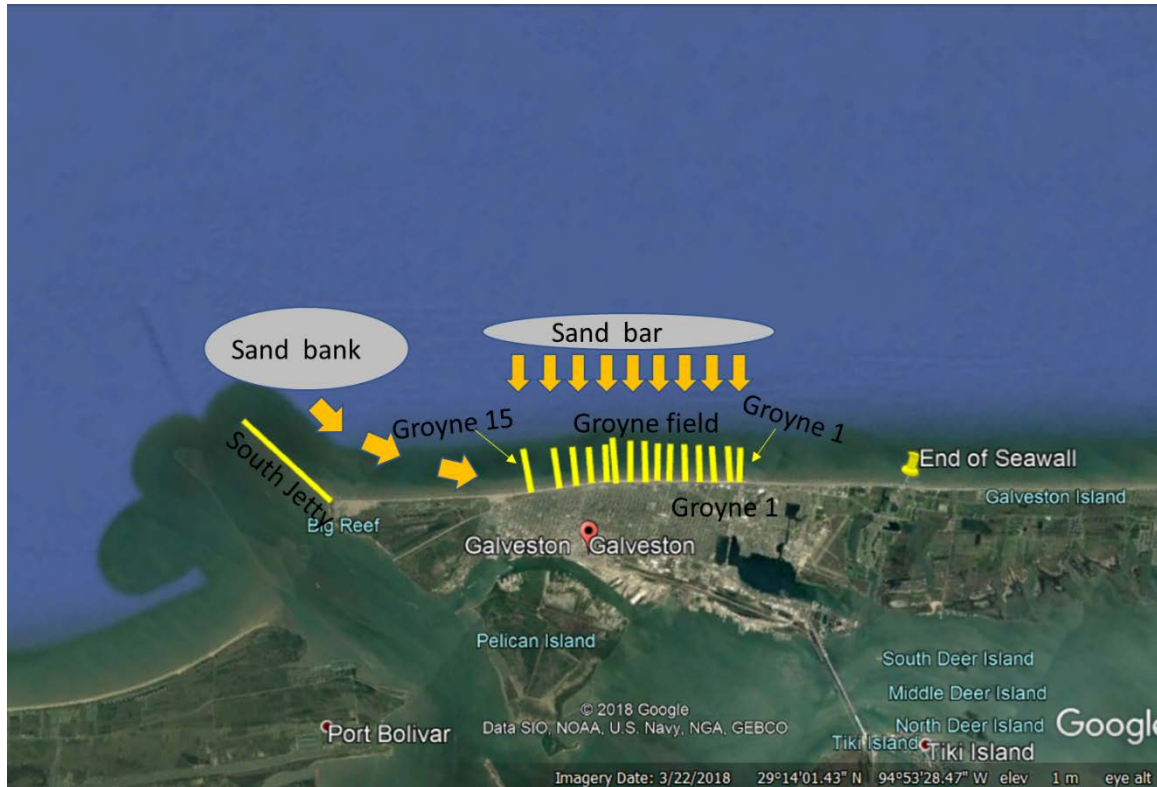


Fig. 14. (a) A decreasing rate of sediment flux  $q_l$  coming from a linear source of sediment material, was considered in the first groyne compartment between South Jetty and Groyne 15. Different time series of sediment flux were tested in the range between  $q_{min}$  and  $q_{max}$ ; (b) The corresponding shoreline positions for  $q_{min}$ ,  $q_{max}$  and  $q_l$  produced RMSE values of 28.77m, 26.85m and 20.66m, respectively.

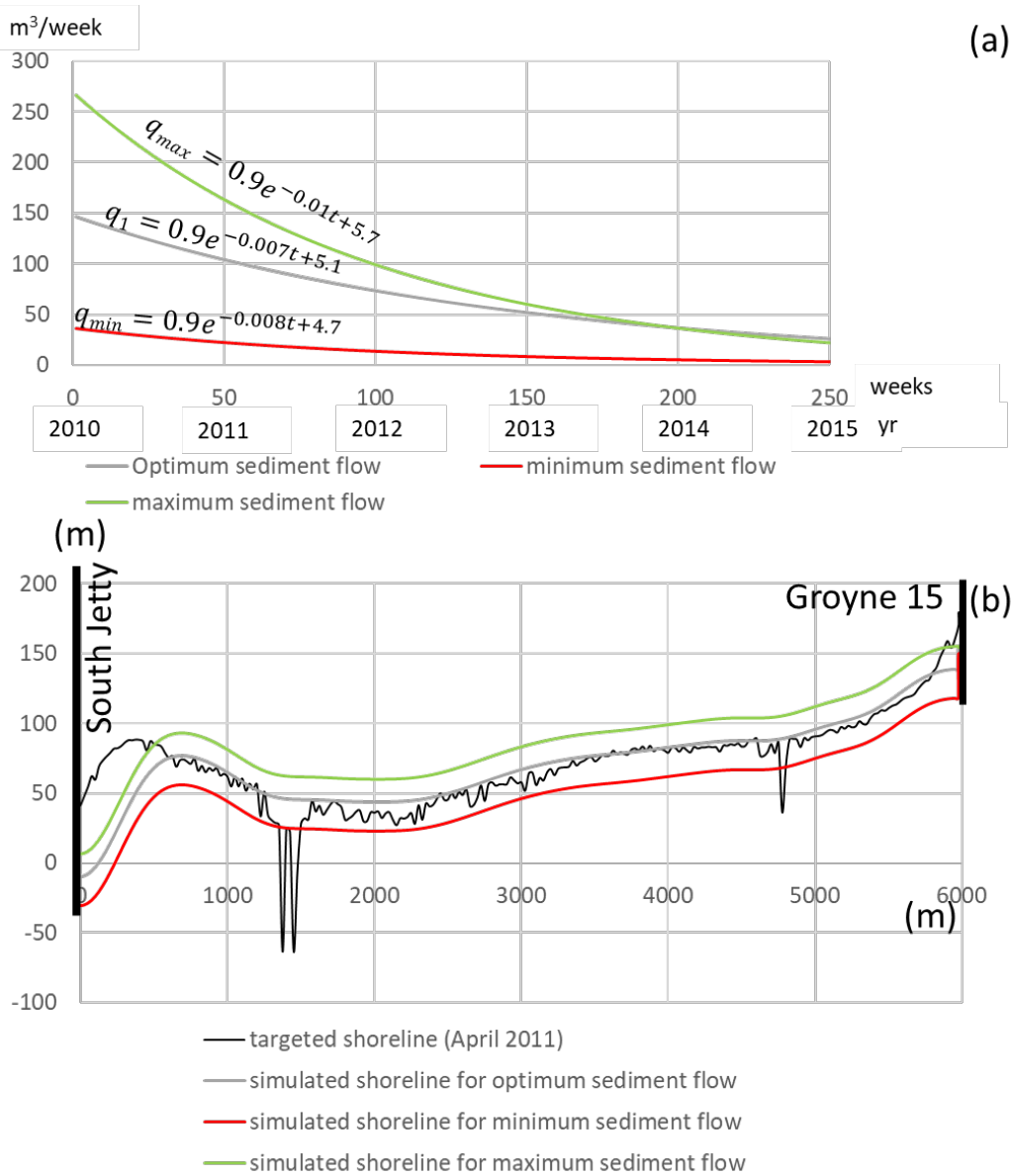


Fig. 15. Best case Scenario 2 solution for the time period: April 2010 – April 2011. (a) The blue line represents the initial shoreline position in April 2010, the orange one the targeted shoreline position in April 2011 and the grey line the simulated shoreline in April 2011. (b) The corresponding relative shorelines, considering the reference shoreline in August 2008.

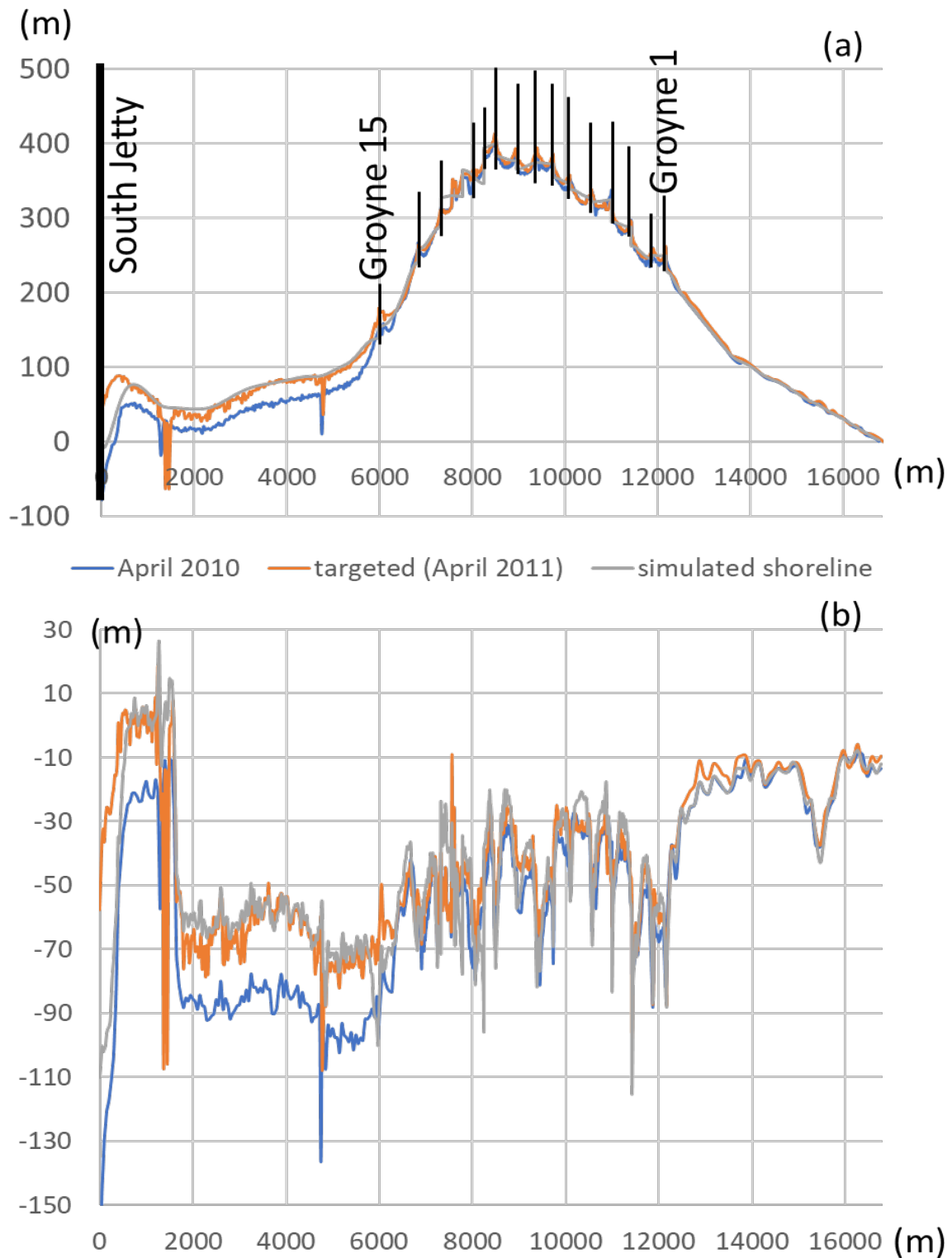




Fig. 16. Validation of the semi-analytical solution in the time period: April 2011 – May 2015. (a) The blue line represents the initial shoreline position in April 2011, the orange one the targeted shoreline position in April 2015 and the gray line the simulated shoreline in May 2015. (b) The corresponding relative shorelines, considering the reference shoreline in August 2008.

