



Swansea University  
Prifysgol Abertawe



## Cronfa - Swansea University Open Access Repository

---

This is an author produced version of a paper published in:  
*ACS Applied Energy Materials*

Cronfa URL for this paper:  
<http://cronfa.swan.ac.uk/Record/cronfa50391>

---

### **Paper:**

Forster, S., Chaussende, D. & Kalna, K. (2019). Monte Carlo Simulations of Electron Transport Characteristics of Ternary Carbide Al<sub>4</sub>SiC<sub>4</sub>. *ACS Applied Energy Materials*, 2(1), 715-720.  
<http://dx.doi.org/10.1021/acsaem.8b01767>

---

This item is brought to you by Swansea University. Any person downloading material is agreeing to abide by the terms of the repository licence. Copies of full text items may be used or reproduced in any format or medium, without prior permission for personal research or study, educational or non-commercial purposes only. The copyright for any work remains with the original author unless otherwise specified. The full-text must not be sold in any format or medium without the formal permission of the copyright holder.

Permission for multiple reproductions should be obtained from the original author.

Authors are personally responsible for adhering to copyright and publisher restrictions when uploading content to the repository.

<http://www.swansea.ac.uk/library/researchsupport/ris-support/>

# Monte Carlo Simulations of Electron Transport Characteristics of Ternary Carbide $\text{Al}_4\text{SiC}_4$

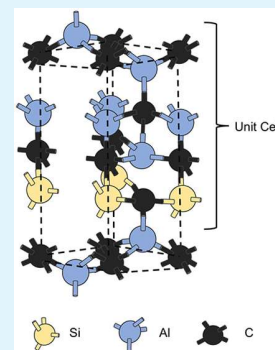
Simon Forster,<sup>\*,†,‡</sup> Didier Chaussende,<sup>‡</sup> and Karol Kalna<sup>†</sup>

<sup>†</sup>Nanoelectronic Devices Computational (NanoDeCo) Group, College of Engineering, Swansea University, Swansea SA1 8EN, Wales, United Kingdom

<sup>‡</sup>Université Grenoble Alpes, CNRS, Grenoble INP, SIMAP, 38000 Grenoble, France

**ABSTRACT:** Electron transport characteristics of a novel wide band gap ternary carbide,  $\text{Al}_4\text{SiC}_4$ , to be used for efficient power and optoelectronic applications, are predicted using ensemble Monte Carlo (MC) simulations. The MC simulations use a mixture of material parameters obtained from density functional theory (DFT) calculations and experiment, with a preference for the experimental data if they are known. The DFT calculations predict a band gap of 2.48 eV, while the experimental measurements give a band gap between 2.78 and 2.8 eV. We have found that the electron effective mass in the two lowest valleys ( $M$  and  $K$ ) is highly anisotropic; in the  $K$  valley,  $m_i^* = 0.5678 m_e$  and  $m_j^* = 0.6952 m_e$ , and for the  $M$  valley,  $m_i^* = 0.9360 m_e$  and  $m_j^* = 1.0569 m_e$ . We simulate electron drift velocity and electron mobility as a function of applied electric field as well as electron mobility as a function of doping concentration in  $\text{Al}_4\text{SiC}_4$ . We predict a peak electron drift velocity of  $1.35 \times 10^7 \text{ cm s}^{-1}$  at an electric field of  $1400 \text{ kV cm}^{-1}$  and a maximum electron mobility of  $82.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ . We have seen diffusion constants of  $2.14 \text{ cm}^2 \text{ s}^{-1}$  at a low electric field and  $0.25 \text{ cm}^2 \text{ s}^{-1}$  at a high electric field. Finally, we show that  $\text{Al}_4\text{SiC}_4$  has a critical field of  $1831 \text{ kV cm}^{-1}$ .

**KEYWORDS:** ensemble Monte Carlo, ternary carbide,  $\text{Al}_4\text{SiC}_4$ , effective mass, electron transport, breakdown



## 1. INTRODUCTION

$\text{Al}_4\text{SiC}_4$ , a wide band gap ternary carbide semiconductor material, has attracted a great deal of interest from the electronics industry over the past decade because of its emerging semiconductor properties, a departure from its previous classification as a ceramic material.<sup>1,2</sup> Although the material was first computed as having a band gap of only 1.05 eV,<sup>3</sup> the band gap has been re-evaluated to be 2.48 eV<sup>4–6</sup> in recent years. This has led to  $\text{Al}_4\text{SiC}_4$  being classified as a wide band gap semiconductor, with a band gap very close to that of, for instance, 3C-SiC and thus potentially addressing similar fields of applications. Other properties that have been documented for this material include superior oxidation resistance,<sup>7,8</sup> superior wear resistance, low weight, high strength, and high thermal conductivity.<sup>9</sup> These material properties mean that  $\text{Al}_4\text{SiC}_4$  could become a very useful and versatile material in applications for the optoelectronics and power electronics industry.

$\text{Al}_4\text{SiC}_4$  is currently being studied by several research groups<sup>5,7,8,10–14</sup> that are looking to find a practical way to fabricate the material in crystalline form.<sup>15</sup> Theoretical investigations, primarily density functional theory (DFT) calculations of a band structure, have been carried out for  $\text{Al}_4\text{SiC}_4$ <sup>2–4,16,17</sup> to determine its material properties and assist in experimental characterization. Other investigations have looked at the optical, ac electrical, thermal, and some mechanical properties of  $\text{Al}_4\text{SiC}_4$ ,<sup>16,18</sup> including a combined study of the structural and mechanical properties of  $\text{Al}_4\text{SiC}_4$ .<sup>1</sup> Dunia et al.<sup>18</sup> examined the electrical properties of Al-SiC

composites with measured values for the ac electrical conductivity and dielectric constant over a frequency range of 200 Hz to 6 GHz. They suggest two frequency-dependent mechanisms for conduction in Al-SiC composites along with dielectric constants following a semi-steady state behavior over the frequency range. Liao et al.<sup>1</sup> investigated the bonding characteristics, elastic stiffness, and ideal strength showing that the mechanical properties are closely related to the crystal structure of  $\text{Al}_4\text{SiC}_4$  giving a bulk modulus of 179 GPa, a shear modulus of 140 GPa, and lattice parameters of  $a = 3.222 \text{ \AA}$  and  $c = 21.352 \text{ \AA}$ . Similar mechanical properties were described by Sun et al.<sup>16</sup> and Liao et al.<sup>1</sup> with additional investigation into the thermal properties of  $\text{Al}_4\text{SiC}_4$ . The heat capacity was shown over a temperature range of 200–2000 K, where the heat capacity rapidly increased at low temperatures while the rate of change slowed at high temperatures (>500 K).

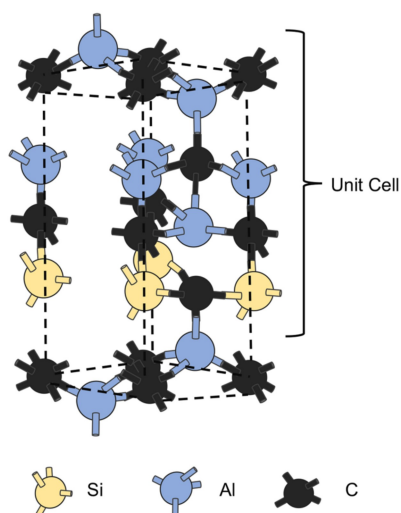
In this work, we have employed an in-house bulk ensemble Monte Carlo (MC) simulation code<sup>19,20</sup> to determine the electron transport properties of  $\text{Al}_4\text{SiC}_4$ . The MC simulations use a combination of known material properties from reported experimental data and theoretical calculations using DFT. Detailed predictions of the electronic transport properties of  $\text{Al}_4\text{SiC}_4$  are completely missing from the literature.

$\text{Al}_4\text{SiC}_4$  has a hexagonal lattice<sup>3–6,14,21,22</sup> comprising multiple valleys,  $\Gamma$ ,  $A$ ,  $L$ ,  $H$ ,  $M$ , and  $K$ , as shown in Figure 1 and

**Received:** October 18, 2018

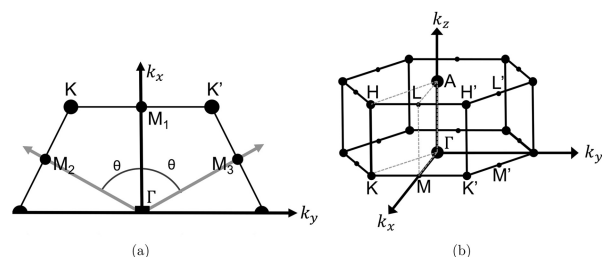
**Accepted:** December 14, 2018

**Published:** December 14, 2018



**Figure 1.** Crystal structures of  $\text{Al}_4\text{SiC}_4$ . The blue, yellow, and black spheres represent Al, Si, and C atoms, respectively.

panels a and b of Figure 2. We will demonstrate that only the two lowest valleys, the M and K valleys, are of interest for



**Figure 2.** (a) Hexagonal (0001) plane showing the location of the M valleys within the  $\text{Al}_4\text{SiC}_4$  hexagonal structure, where  $\theta = \pm 60^\circ$ . (b) Hexagonal structure showing the location of principal valleys.

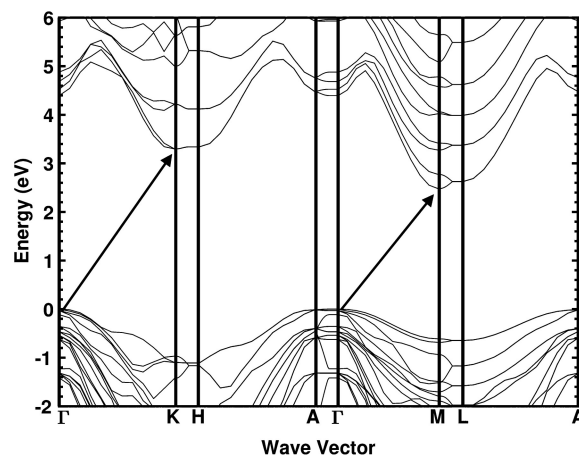
electron transport as the occupation of all other upper valleys is negligible. The MC simulations predict that  $\text{Al}_4\text{SiC}_4$  will have a maximum electron drift velocity of  $1.35 \times 10^7 \text{ cm s}^{-1}$  at an electric field of  $1400 \text{ kV cm}^{-1}$  and a maximum electron mobility of  $82.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ . We also show what is the dependence of the electron mobility on the ionized impurity concentration in  $\text{Al}_4\text{SiC}_4$ . We predict a steady diffusion constant of approximately  $0.25 \text{ cm}^2 \text{ s}^{-1}$  at a high electric field of  $1400 \text{ kV cm}^{-1}$ . Finally, we show that the critical field for  $\text{Al}_4\text{SiC}_4$  is  $1831 \text{ kV cm}^{-1}$ .

The paper is organized as follows. Section 2 gives details about material parameters and the physical model used, a bulk ensemble MC simulation. Section 3 outlines a rotational valley transformation that has been introduced in this work for the particular band structure of  $\text{Al}_4\text{SiC}_4$ . Section 4 presents the results and discusses them. Finally, section 5 draws a conclusion.

## 2. MONTE CARLO SIMULATIONS

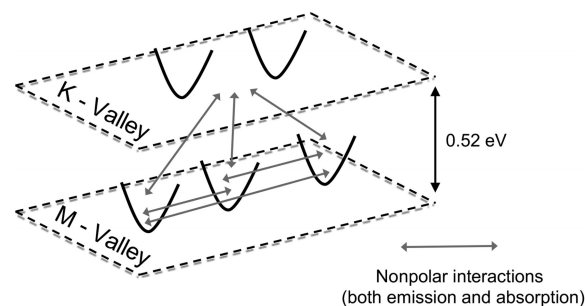
We have adapted an ensemble bulk MC simulation code to investigate the electron transport in bulk  $\text{Al}_4\text{SiC}_4$ . The simulation considers bulk properties of  $\text{Al}_4\text{SiC}_4$  when electron transport can be considered to be free in three-dimensional  $\mathbf{k}$  space. We have employed a two-valley model for the conduction band of  $\text{Al}_4\text{SiC}_4$  based on the band structure

obtained by Pedesseau et al.<sup>4</sup> as seen in Figure 3. The two arrows in this figure indicate the two valleys that we are



**Figure 3.** Rescaled  $\text{Al}_4\text{SiC}_4$  band structure obtained from DFT calculations from ref 4. The two black arrows indicate the two valleys that we considered in the MC simulations.

considering in a simulation model. The first valley, the M valley, is situated 2.78 eV above the valence band maximum of the  $\Gamma$  valley and is an indirect band gap. The second valley, the K valley, is situated 0.52 eV above the M valley (see Figure 4) and has also an indirect band gap.



**Figure 4.** Schematic of conduction band minimum valleys in  $\text{Al}_4\text{SiC}_4$  showing the number of equivalent bands in each valley and the separation between the two considered valleys.

However, to date this band gap has been estimated to be anywhere between 1.05 and 2.5 eV according to various authors who have published their work on  $\text{Al}_4\text{SiC}_4$ . A summary of these works is shown in Table 1, indicating the value of the band gap. We have chosen to use the value of 2.78 eV for the

**Table 1. Comparison of Published Energy Band Gaps for  $\text{Al}_4\text{SiC}_4$  Indicating a Method and a Source**

published band gap (eV)	method
1.05	computational (DFT) <sup>3</sup>
1.12	computational (DFT) <sup>16</sup>
1.81	computational (DFT) <sup>17</sup>
2–2.5	experiment (UV–vis–NIR) <sup>5</sup>
2.48	computational (DFT), experimental (ellipsometry) <sup>4</sup>
2.4–2.5	experiment (UV–vis–NIR and ellipsometry) <sup>6</sup>

band gap as this has been obtained in our experimental work.<sup>23</sup> A majority of the DFT simulations to date have shown a lower value for the band gap of <2.0 eV, which is an underestimation of the band gap often observed in DFT calculations of wide band gap materials.<sup>24</sup>

Figure 4 includes the number of equivalent bands that have been identified for the two valleys of interest for MC simulations. The number of equivalent valleys in each of the two valleys is based on the hexagonal lattice that Al<sub>4</sub>SiC<sub>4</sub> is known to have.<sup>3–6,14,21,22</sup> Figure 2a shows that the *K* valley is present in six locations, each of which contributes one-third to the first Brillouin zone leading to a total of two equivalent bands. The *M* valley is present in six locations similar to the *K* valleys. However, because of their positions between the *K* valleys, each of these six *M* valleys contributes one-half to the first Brillouin zone, leading to a total of three equivalent bands. The band structure model of Al<sub>4</sub>SiC<sub>4</sub> is an analytical nonparabolic anisotropic band structure.<sup>25</sup> We have considered the following electron scattering mechanisms in the MC simulations that will play a decisive role in electron transport (see Table 2): electron interactions with acoustic phonons,

**Table 2. Electron–Phonon Scattering Transitions Considered in the MC Model**

valley	scattering between	polar or nonpolar	inter- or intravalley
<i>M</i> <sub>1</sub>	<i>M</i> <sub>1</sub> → <i>M</i> <sub>1</sub>	polar	intra
	<i>M</i> <sub>1</sub> → <i>M</i> <sub>1</sub>	polar	intra
	<i>M</i> <sub>1</sub> → <i>M</i> <sub>2</sub>	nonpolar	inter
	<i>M</i> <sub>1</sub> → <i>M</i> <sub>3</sub>	nonpolar	inter
	<i>M</i> <sub>1</sub> → <i>K</i>	nonpolar	inter
<i>M</i> <sub>2</sub>	<i>M</i> <sub>2</sub> → <i>M</i> <sub>2</sub>	polar	intra
	<i>M</i> <sub>2</sub> → <i>M</i> <sub>2</sub>	polar	intra
	<i>M</i> <sub>2</sub> → <i>M</i> <sub>1</sub>	nonpolar	inter
	<i>M</i> <sub>2</sub> → <i>M</i> <sub>3</sub>	nonpolar	inter
	<i>M</i> <sub>2</sub> → <i>K</i>	nonpolar	inter
<i>M</i> <sub>3</sub>	<i>M</i> <sub>3</sub> → <i>M</i> <sub>3</sub>	polar	intra
	<i>M</i> <sub>3</sub> → <i>M</i> <sub>3</sub>	polar	intra
	<i>M</i> <sub>3</sub> → <i>M</i> <sub>1</sub>	nonpolar	inter
	<i>M</i> <sub>3</sub> → <i>M</i> <sub>2</sub>	nonpolar	inter
	<i>M</i> <sub>3</sub> → <i>K</i>	nonpolar	inter
<i>K</i>	<i>K</i> → <i>M</i> <sub>1</sub>	nonpolar	inter
	<i>K</i> → <i>M</i> <sub>2</sub>	nonpolar	inter
	<i>K</i> → <i>M</i> <sub>3</sub>	nonpolar	inter

with polar and nonpolar optical phonons, and with ionized impurities when simulating electron transport properties in an n-type doped Al<sub>4</sub>SiC<sub>4</sub>.

The MC simulations assume a crystal temperature at 300 K and the orientation of the applied electric field along the ⟨0001⟩ crystallographic direction of the hexagonal lattice structure.<sup>3–6,14,21,22</sup> The material parameters, including parameters for electron–phonon interactions, are listed in Table 3. In the case of acoustic deformation potential, we have opted for the value reported for 4H-SiC<sup>26</sup> as the closest semiconductor material to Al<sub>4</sub>SiC<sub>4</sub> with a well-known electron–phonon deformation potential because an acoustic deformation potential is currently unknown in Al<sub>4</sub>SiC<sub>4</sub>.

A critical electric field of Al<sub>4</sub>SiC<sub>4</sub> is calculated using eq 1 as<sup>27</sup>

$$\varepsilon_c = a(E_G)^n \quad (1)$$

where  $a = 2.3818 \times 10^5$  and  $n = 1.995$  for an indirect band gap semiconductor and  $E_G$  is the band gap of the semiconductor.

**Table 3. Material Parameters of Al<sub>4</sub>SiC<sub>4</sub>**

mass density (g/cm <sup>3</sup> )	3.03 <sup>a</sup>
lattice constant (Å)	3.28 <sup>a</sup>
piezoelectric constant (C/m <sup>2</sup> )	0.47 <sup>a</sup>
longitudinal acoustic velocity (m/s)	10577 <sup>a</sup>
transverse acoustic velocity (m/s)	6431 <sup>a</sup>
polar optical phonon energies (meV)	67.32, <sup>b</sup> 107.24 <sup>b</sup>
nonpolar optical phonon energy (meV)	85.55 <sup>b</sup>
acoustic deformation potential (eV)	11.4q <sup>c</sup>
indirect band gap (eV)	$E_G^{(M)} = 2.78$ <i>M</i> valley $E_G^{(K)} = 3.30$ <i>K</i> valley
electron effective mass	$m_i^{*(M)} = 0.5678$ $m_e^d$
	$m_i^{*(M)} = 0.6952$ $m_e^d$
	$m_i^{*(K)} = 1.0569$ $m_e^d$
	$m_i^{*(K)} = 0.9360$ $m_e^d$

<sup>a</sup>From ref 4. <sup>b</sup>From ref 5. <sup>c</sup>Average taken from ref 26. <sup>d</sup>Extracted value from DFT calculations.<sup>4</sup>

Assuming a band gap of 2.78 eV, we obtain a critical electric field of 1831 kV cm<sup>-1</sup> for Al<sub>4</sub>SiC<sub>4</sub>. This critical electric field is well below the maximum electric field of 1400 kV cm<sup>-1</sup> we have simulated.

The optical phonon energies that have been used in these simulations have been extracted from IR/Raman spectroscopy from the works of Zevgitis et al.<sup>7</sup> Here, we have taken the three highest peaks in the *Z*(*XX*)*Z* polarization configuration, where one would expect to see only *A*<sub>1</sub> and *E*<sub>2</sub> modes. The first peak we have taken is at a wavenumber of 690 cm<sup>-1</sup>, which relates to an energy of 85.55 meV, and is an *E*<sub>2</sub> nonpolar mode, longitudinal optical phonon. The second peak is at a wavenumber of 543 cm<sup>-1</sup>, which relates to an energy of 67.32 meV, and is an *A*<sub>1</sub> polar mode, transverse optical phonon. Finally, the third peak is at a wavenumber of 865 cm<sup>-1</sup>, which relates to an energy of 107.25 meV, and is an *A*<sub>1</sub> polar mode, longitudinal optical phonon.

At the moment, a specific relationship between vibrational states and electrons is not clear with respect to which vibrational states directly contribute to or hinder the electron mobility. The electron effective masses in Table 3 have been extracted from DFT calculations by Pedesseau et al.<sup>4</sup> Here, we have assumed that the minima of the conduction band have a parabolic energy dispersion. The relative effective mass,  $m^*$ , can be then extracted from the following relation:

$$\frac{1}{m^*} = \frac{1}{\hbar^2} \frac{\partial^2 E(\vec{k})}{\partial k^2} \quad (2)$$

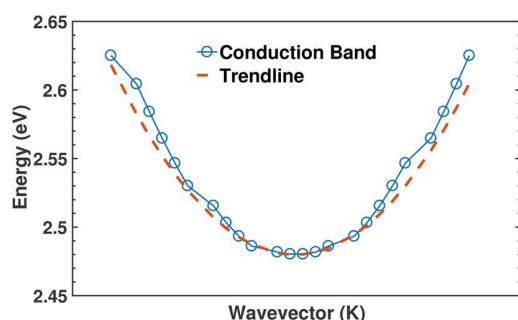
The dispersion relation is a quadratic polynomial, as illustrated in Figure 5, in the form  $y = b + c_1x + c_2x^2$ . The second-order derivative,  $2c_2$ , is related to the energy dispersion relation in eq 2 as

$$2c_2 = \frac{\partial^2 E(\vec{k})}{\partial k^2} \quad (3)$$

Equation 2 is solved for the *M* and *K* valleys in both the longitudinal and transverse directions giving the values of relative effective masses shown in Table 3.

### 3. WAVE-VECTOR TRANSFORMATIONS FOR THE *M* VALLEY

The location of the principal electron valley, *M*, in the Brillouin zone requires that components of electron wave-vectors in the



**Figure 5.** Dispersion relation in a conduction band fitted with a polynomial trend line.

band structure anisotropic analytical model of MC simulations be transformed accordingly. Therefore, we have enhanced our MC code with the wave-vector transformations that include a combination of Herring–Vogt transformation<sup>28</sup> and a rotational transformation of valleys.

The rotational transformation applied to the  $M$  valleys looks at transforming from elliptical space  $k$ -vector components,  $k_x$ ,  $k_y$ , and  $k_z$ , to spherical vector components,  $k_x^*$ ,  $k_y^*$ , and  $k_z^*$ , while considering the angular distance that the  $M_2$  and  $M_3$  valleys have in relation to the  $M_1$  valley, our reference valley, located along the  $k_x$  direction as illustrated in Figure 2a. The angular distance that the  $M_2$  and  $M_3$  valleys have in relation to the  $M_1$  valley can be defined along the  $k_x$  and  $k_y$  axes, as these valleys are rotated about the  $k_z$  axis (the  $k_z$  axis does not need to be transformed). The  $k$ -vector transformations for each of the components are defined as

$$k_x^* = k_x \cos(\theta) - k_y \sin(\theta) \quad (4)$$

$$k_y^* = k_y \cos(\theta) + k_x \sin(\theta) \quad (5)$$

$$k_z^* = k_z \quad (6)$$

In eqs 4–9,  $\theta$  represents the angular distance the  $M_2$  or  $M_3$  valley rotates from the  $M_1$  valley. The inverse transformations are given by

$$k_x = k_x^* \cos(\theta) + k_y^* \sin(\theta) \quad (7)$$

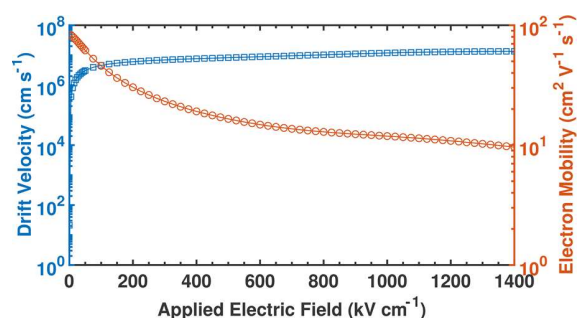
$$k_y = k_y^* \cos(\theta) - k_x^* \sin(\theta) \quad (8)$$

$$k_z = k_z^* \quad (9)$$

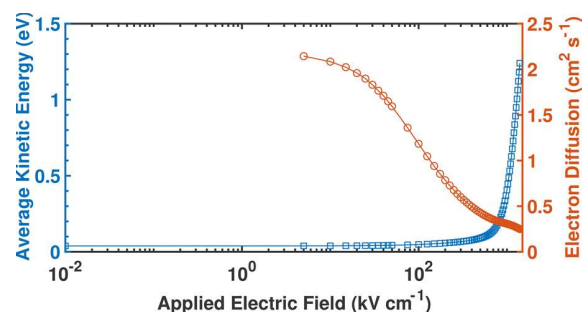
Finally, we assume an isotropic valley approximation for the  $K$  valleys due to their low electron occupation.

#### 4. ELECTRON TRANSPORT PROPERTIES OF $\text{Al}_4\text{SiC}_4$

Figure 6 illustrates the electron drift velocity as a function of the applied electric field. The figure shows the applied electric field in a range from 0.01 to 1400  $\text{kV cm}^{-1}$ . The electron velocity increases with an increasing electric field quickly at a relatively low electric field and starts to saturate at an electric field of  $\sim 200 \text{ kV cm}^{-1}$ . At an applied electric field of 1400  $\text{kV cm}^{-1}$ , the maximum drift velocity is approximately  $1.35 \times 10^7 \text{ cm s}^{-1}$ , at which point the electron velocity is very well saturated. This saturation is caused by a strong emission of two polar optical phonons at energies of 67 and 107 meV (see Table 3). The average kinetic energy as a function of applied electric field is plotted in Figure 7. The kinetic energy increases

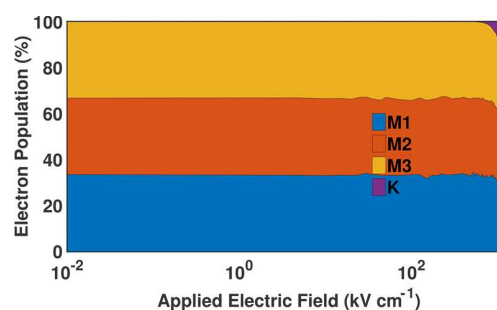


**Figure 6.** Electron drift velocity (blue squares) as a function of applied electric field in bulk  $\text{Al}_4\text{SiC}_4$  on the left axis. Electron mobility (red circles) as a function of applied electric field in bulk  $\text{Al}_4\text{SiC}_4$  on the right axis.



**Figure 7.** Average electron kinetic energy (blue squares) as a function of the applied electric field in bulk  $\text{Al}_4\text{SiC}_4$  at the left. Electron diffusion (red circles) as a function of the applied electric field in bulk  $\text{Al}_4\text{SiC}_4$  at the right.

approximately linearly as the electric field increases considering that the electric field is plotted on a logarithmic scale. We have monitored the electron kinetic energy that is larger than the band gap of  $\text{Al}_4\text{SiC}_4$  in the simulations. At the largest electric field of 1400  $\text{kV cm}^{-1}$  occurring in the simulations in Figures 7 and 8, the number of electrons over this energy amounts to



**Figure 8.** Stacked plot of the calculated valley occupancy of electrons in the three  $M$  and  $K$  valleys as a function of the applied electric field in bulk  $\text{Al}_4\text{SiC}_4$ .

0.119% of the total number of electrons simulated. This indicates that electron transport in the material is close to a breakdown due to excessive impact ionization at an electric field of 1400  $\text{kV cm}^{-1}$ . This result indicating onset of impact ionization supports our calculated critical electric field of 1831  $\text{kV cm}^{-1}$ .

Figures 6 and 7 show electron diffusion and electron mobility as a function of the applied electric field, respectively.

The electron mobility and the electron diffusion decay exponentially as the electric field increases. The electron mobility and electron diffusion at a low electric field are  $82.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  and  $2.1 \text{ cm}^2 \text{ s}^{-1}$ , respectively, which are at their respective maxima, while at a high electric field of  $1400 \text{ kV cm}^{-1}$ , the values are  $9.63 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  and  $0.25 \text{ cm}^2 \text{ s}^{-1}$ , respectively.

Figure 8 shows a stacked plot to illustrate the population of electrons occupying each valley (*M* and *K* valleys) obtained from the MC simulations. The *M* valley becomes populated evenly at the start of the simulation as expected until the electrons have enough energy to make a transition into the *K* valley. The *K* valley does not start to become populated until approximately  $450 \text{ kV cm}^{-1}$  but remains <20% populated at the largest electric field, which justifies our approximation of an isotropic *K* valley.

Finally, we examine the relationship between electron mobility and ionized impurity concentration in Figure 9. The

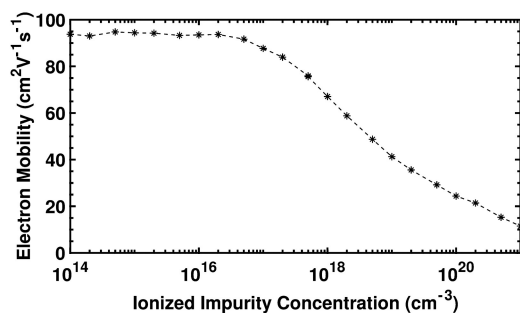


Figure 9. Electron mobility as a function of ionized impurity concentration in bulk  $\text{Al}_4\text{SiC}_4$ .

electron mobility of  $\text{Al}_4\text{SiC}_4$  has a typical dependence on the ionized impurity concentration when the mobility remains approximately constant until an ionized impurity concentration of  $2 \times 10^{16} \text{ cm}^{-3}$  is reached. When the ionized impurity concentration increases further, the electron mobility starts to decline to  $\sim 10 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  as seen in many semiconductor materials.<sup>20</sup>

## 5. CONCLUSIONS

The MC simulations of the electron transport in  $\text{Al}_4\text{SiC}_4$  that has a hexagonal crystal structure have been adapted to include a rotational transformation in the lowest conduction band, the *M* valley, to account for the strong anisotropy of the electron effective mass. The strong anisotropy of the electron effective mass in the *M* valley has a profound impact on the electron drift velocity and mobility. The electron effective masses extracted from DFT calculations have shown that there is a large effective mass in both the longitudinal and transverse directions for the *K* valley of 1.0569 and  $0.9360 m_0$ , respectively, compared with those for the *M* valley of 0.5678 and  $0.6952 m_0$ , respectively.

The MC simulations allow us to predict the material transport properties of  $\text{Al}_4\text{SiC}_4$ . We have predicted the dependence of the electron drift velocity, electron mobility, average kinetic energy of electrons, and electron population against the applied electric field, all of which can serve as crucial indicators in assessing the electronic and optoelectronic performance of devices. We have shown that the electron drift velocity increases with an increase in the electric field reaching

$1.35 \times 10^7 \text{ cm s}^{-1}$  to approximately  $1400 \text{ kV cm}^{-1}$ . The electron kinetic energy has a linear increase as expected and reaches  $1.24 \text{ eV}$  at  $1400 \text{ kV cm}^{-1}$ . The threshold energy barrier when electrons start to be transferred from the *M* valley to the *K* valley occurs at an electric field of approximately  $450 \text{ kV cm}^{-1}$ . We predict that the number of electrons with a higher energy that is greater than the band gap of the material will start to increase rapidly as the electric field draws closer to the critical field of  $1831 \text{ kV cm}^{-1}$ , causing a breakdown to occur.

The electron mobility decreases with an increase in the electric field from approximately  $82.9$  to  $9.6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , and the diffusion decreases from approximately  $2.14$  to  $0.25 \text{ cm}^2 \text{ s}^{-1}$ , both over a range of very low electric fields to  $1400 \text{ kV cm}^{-1}$ . Finally, we have shown that the electron mobility is dependent on the ionized impurity concentration, declining from its maximum value of  $82.9 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at low doping concentrations of  $\leq 2 \times 10^{16} \text{ cm}^{-3}$  to  $\sim 10 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at a very high doping concentration of  $10^{21} \text{ cm}^{-3}$ . These predicted material properties show a limited usage of the  $\text{Al}_4\text{SiC}_4$  in a channel of potential metal oxide semiconductor field effect transistors (MOSFETs) due to a maximum drift velocity and electron mobility of  $1.35 \times 10^7 \text{ cm s}^{-1}$  and  $83 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ , respectively. Upon comparison of these two material properties of  $\text{Al}_4\text{SiC}_4$  with properties of known semiconductor materials, the maximum drift velocity of  $\text{Al}_4\text{SiC}_4$  is only 61.4% of the maximum drift velocity of GaN ( $2.2 \times 10^7 \text{ cm s}^{-1}$ ) and the electron mobility of  $\text{Al}_4\text{SiC}_4$  is 6.7% of the electron mobility of GaN ( $1250 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ).<sup>29</sup> The maximum drift velocity of  $\text{Al}_4\text{SiC}_4$  is only 67.5% of that of 6H-SiC ( $2 \times 10^7 \text{ cm s}^{-1}$ ), and the electron mobility of  $\text{Al}_4\text{SiC}_4$  is only 16.6% of that of 6H-SiC ( $500 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ).<sup>29</sup> Finally, the maximum drift velocity of  $\text{Al}_4\text{SiC}_4$  is 135% of that of silicon ( $1 \times 10^7 \text{ cm s}^{-1}$ ) and the electron mobility of  $\text{Al}_4\text{SiC}_4$  is only 5.5% of that of silicon ( $1500 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ).<sup>29</sup>

## AUTHOR INFORMATION

### Corresponding Author

\*E-mail: [s.forster.661270@swansea.ac.uk](mailto:s.forster.661270@swansea.ac.uk).

### ORCID

Simon Forster: 0000-0002-5285-4353

Didier Chaussende: 0000-0002-4180-8749

### Notes

The authors declare no competing financial interest.

## ACKNOWLEDGMENTS

The authors acknowledge Dr. Laurent Pedesseau for having provided the raw data of DFT calculations previously reported,<sup>4</sup> which have been used in this work.

## REFERENCES

- (1) Liao, T.; Wang, J.; Zhou, Y. Atomistic deformation modes and intrinsic brittleness of  $\text{Al}_4\text{SiC}_4$ : A first-principles investigation. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2006**, *74*, 174112.
- (2) Li, Y. F.; Xiao, B.; Sun, L.; Gao, Y. M.; Cheng, Y. H. Phonon optics, thermal expansion tensor, thermodynamic and chemical bonding properties of  $\text{Al}_4\text{SiC}_4$  and  $\text{Al}_4\text{Si}_2\text{C}_5$ : a first-principles study. *RSC Adv.* **2016**, *6*, 43191–43204.
- (3) Hussain, A.; Aryal, S.; Rulis, P.; Choudhry, M. A.; Ching, W. Y. Density functional calculations of the electronic structure and optical properties of the ternary carbides  $\text{Al}_4\text{SiC}_4$  and  $\text{Al}_4\text{Si}_2\text{C}_5$ . *Phys. Rev. B: Condens. Matter Mater. Phys.* **2008**, *78*, 195102.
- (4) Pedesseau, L.; Even, J.; Modreanu, M.; Chaussende, D.; Sarigiannidou, E.; Chaix-Pluchery, O.; Durand, O.  $\text{Al}_4\text{SiC}_4$  wurtzite

crystal: Structural, optoelectronic, elastic, and piezoelectric properties. *APL Mater.* **2015**, *3*, 121101.

(5) Zevgitis, D.; Chaix-Pluchery, O.; Doineau, B.; Modreanu, M.; La Manna, J.; Sarigiannidou, E.; Chaussende, D. Synthesis and Characterization of Al<sub>4</sub>SiC<sub>4</sub>: A "New" Wide Band Gap Semiconductor. *Mater. Sci. Forum* **2015**, 821-823, 974-977.

(6) Pedesseau, L.; Chaix-Pluchery, O.; Modreanu, M.; Chaussende, D.; Sarigiannidou, E.; Rolland, A.; Even, J.; Durand, O. Al<sub>4</sub>SiC<sub>4</sub> vibrational properties: density functional theory calculations compared to Raman and infrared spectroscopy measurements. *J. Raman Spectrosc.* **2017**, *48*, 891-896.

(7) Inoue, K.; Yamaguchi, A. Synthesis of Al<sub>4</sub>SiC<sub>4</sub>. *J. Am. Ceram. Soc.* **2003**, *86*, 1028-1030.

(8) Inoue, K.; Yamaguchi, A.; Hashimoto, S. Fabrication and oxidation resistance of Al<sub>4</sub>(14)SiC<sub>4</sub>(4) body. *Nippon Seramikusu Kyokai Gakujutsu Ronbunshi* **2002**, *110*, 1010-1015.

(9) Ching, W.; Rulis, P. *Electronic Structure Methods for Complex Materials: The Orthogonalized Linear Combination of Atomic Orbitals*; Oxford University Press: Oxford, U.K., 2012.

(10) Deng, C.; Kuang, J.; Zhu, H.; Bai, C. Effects of Fe<sub>2</sub>O<sub>3</sub> on synthesis of Al<sub>4</sub>SiC<sub>4</sub>/Al<sub>4</sub>O<sub>4</sub>C composite refractory from natural raw materials. *Guisuanyan Xuebao* **2010**, *8*, 049.

(11) Yamaguchi, A.; Zhang, S. Synthesis and some properties of Al<sub>4</sub>SiC<sub>4</sub>. *Nippon Seramikusu Kyokai Gakujutsu Ronbunshi* **1995**, *103*, 20-24.

(12) Zhao, J.; Lin, W.; Yamaguchi, A.; Ommyoji, J.; Sun, J. Synthesis of Al<sub>4</sub>SiC<sub>4</sub> from alumina, silica and graphite. *J. Ceram. Soc. Jpn.* **2007**, *115*, 761-766.

(13) Yamamoto, O.; Ohtani, M.; Sasamoto, T. Preparation and oxidation of Al<sub>4</sub>SiC<sub>4</sub>. *J. Mater. Res.* **2002**, *17*, 774-778.

(14) Schoennahl, J.; Willer, B.; Daire, M. The mixed carbide Al<sub>4</sub>SiC<sub>4</sub> - Preparation and Structural Data. *J. Solid State Chem.* **1984**, *52*, 163-173.

(15) Le-Tran, H.-L.; Sarigiannidou, E.; Gélard, I.; Chaussende, D. Vaporization and condensation in the Al<sub>4</sub>C<sub>3</sub>-SiC system. *J. Eur. Ceram. Soc.* **2017**, *37*, 4475-4482.

(16) Sun, L.; Gao, Y.; Li, Y.; Yoshida, K.; Yano, T.; Yi, D. Structural, bonding, anisotropic mechanical and thermal properties of Al<sub>4</sub>SiC<sub>4</sub> and Al<sub>4</sub>Si<sub>2</sub>C<sub>5</sub> by first-principles investigations. *Journal of Asian Ceramic Societies* **2016**, *4*, 289-298.

(17) Li, Y.; Xiao, B.; Sun, L.; Gao, Y.; Cheng, Y. A theoretical study of dielectric tensor, Born effective charges, LO-TO splitting and infrared response of Al<sub>4</sub>SiC<sub>4</sub> and Al<sub>4</sub>Si<sub>2</sub>C<sub>5</sub>. *J. Alloys Compd.* **2017**, *692*, 713-719.

(18) Al-Nasrawy, D. K. M.; Ahmed Al-Sarraj, Z. S.; Issa, T. T.; Jassim, S. G. H. Observations on the Electrical Properties of Al-SiC Composite. *Journal of Al-Nahrain University-Science* **2012**, *15*, 120-128.

(19) Aldegunde, M.; Kalna, K. Energy conserving, self-force free Monte Carlo simulations of semiconductor devices on unstructured meshes. *Comput. Phys. Commun.* **2015**, *189*, 31-36.

(20) Islam, A.; Kalna, K. Monte Carlo simulations of mobility in doped GaAs using self-consistent fermidirac statistics. *Semicond. Sci. Technol.* **2011**, *26*, 05S007.

(21) Barczak, V. Optical and X-Ray Powder Diffraction Data for Al<sub>4</sub>SiC<sub>4</sub>. *J. Am. Ceram. Soc.* **1961**, *44*, 299.

(22) Solozhenko, V.; Kurakevych, O. Equation of state of aluminum silicon carbide alpha-Al<sub>4</sub>SiC<sub>4</sub>. *Solid State Commun.* **2005**, *135*, 87-89.

(23) Forster, S.; Canas, J.; Lloret, F.; Gutierrez, M.; Araujo, D.; Kalna, K.; Chaussende, D. Experimental Extraction of the Bandgap for Al<sub>4</sub>SiC<sub>4</sub>. *Proceedings of UK Semiconductors*, Sheffield, UK, July 4-5, 2018.

(24) Morales-Garcia, A.; Valero, R.; Illas, F. An Empirical, yet Practical Way To Predict the Band Gap in Solids by Using Density Functional Band Structure Calculations. *J. Phys. Chem. C* **2017**, *121*, 18862-18866.

(25) Elmessary, M. A.; Nagy, D.; Aldegunde, M.; Seoane, N.; Indalecio, G.; Lindberg, J.; Dettmer, W.; Perić, D.; García-Loureiro, A. J.; Kalna, K. Scaling/LER study of Si GAA nanowire FET using 3D

finite element Monte Carlo simulations. *Solid-State Electron.* **2017**, *128*, 17-24.

(26) Iwata, H.; Itoh, K. Donor and acceptor concentration dependence of the electron Hall mobility and the Hall scattering factor in n-type 4H- and 6H-SiC. *J. Appl. Phys.* **2001**, *89*, 6228-6234.

(27) Hudgins, J. L.; Simin, G. S.; Santi, E.; Khan, M. A. An Assessment of Wide Bandgap Semiconductors for Power Devices. *IEEE Transactions on Power Electronics* **2003**, *18*, 907-915.

(28) Herring, C.; Vogt, E. Transport and deformation - potential theory for many-valley semiconductors with anisotropic scattering. *Phys. Rev.* **1956**, *101*, 944-961.

(29) Ozpineci, B.; Tolbert, L. M. Comparison of Wide-Bandgap Semiconductors for Power Electronics Applications. Technical Report ORNL/TM-2003/257; Oak Ridge National Laboratory: Oak Ridge, TN, 2004.